

# Using SPICE Monte Carlo Tool for Statistical Error Analysis

TIPL 4203

TI Precision Labs – ADCs

Created by Art Kay

Presented by Peggy Liska

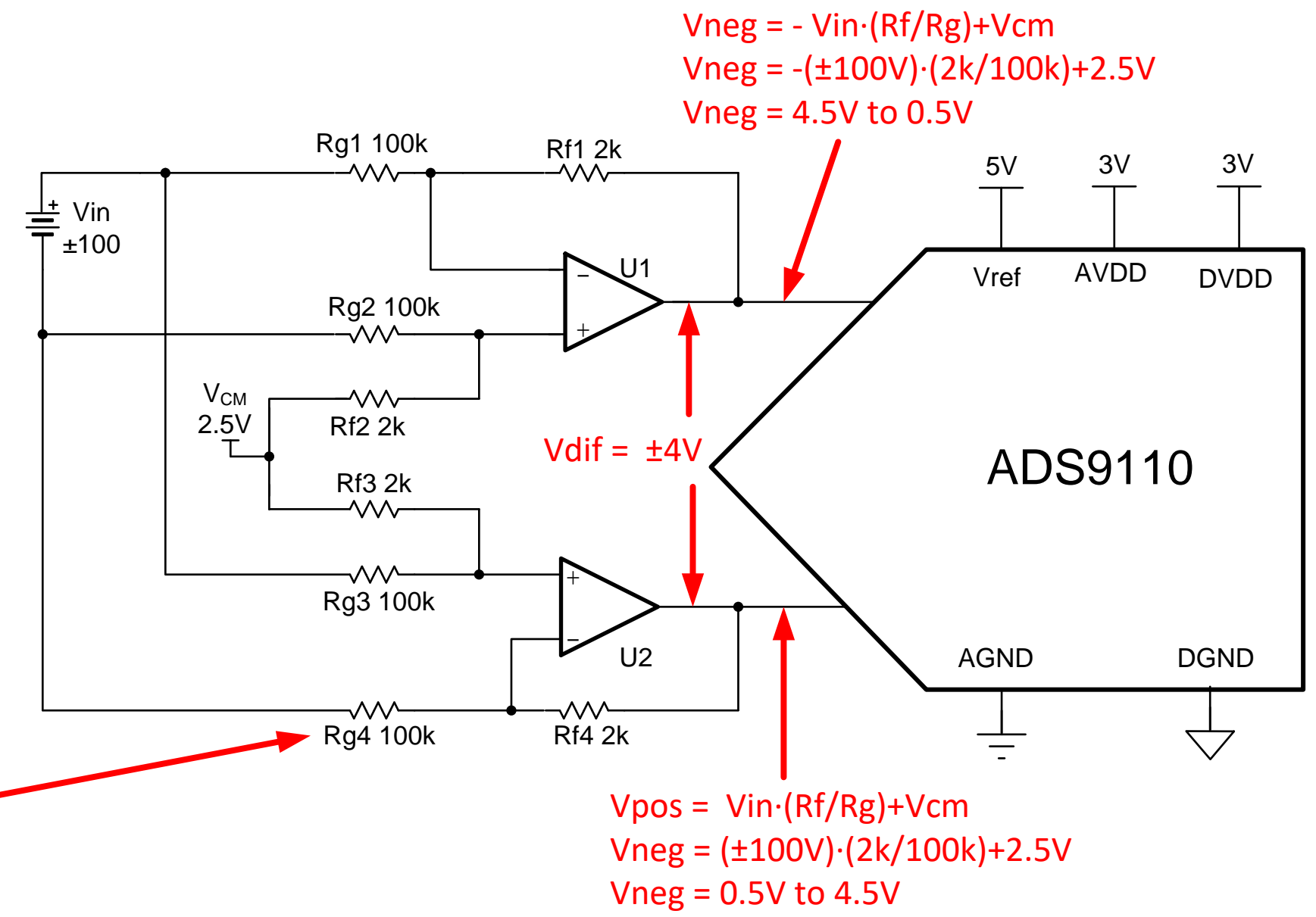
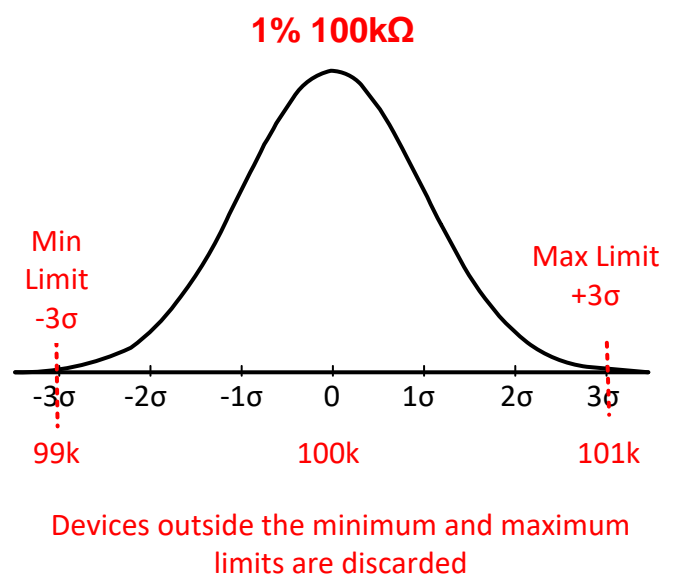
# Discrete resistor tolerance sets gain error

$$G_{diff} = 2 \cdot \left( \frac{R_f}{R_g} \right)$$

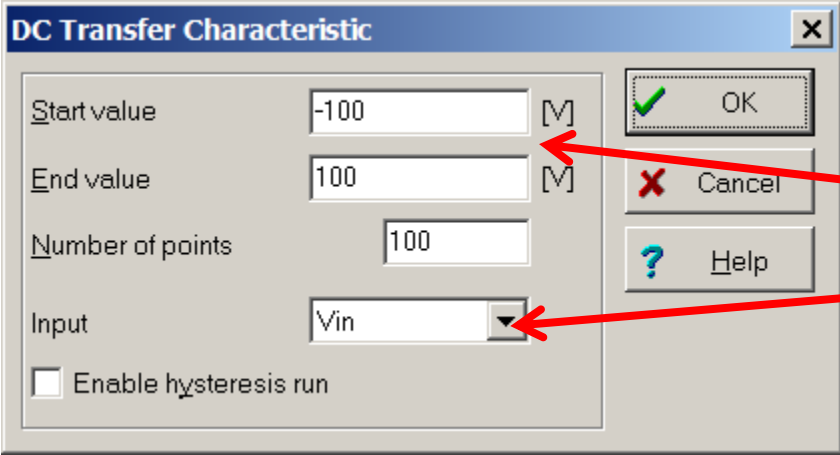
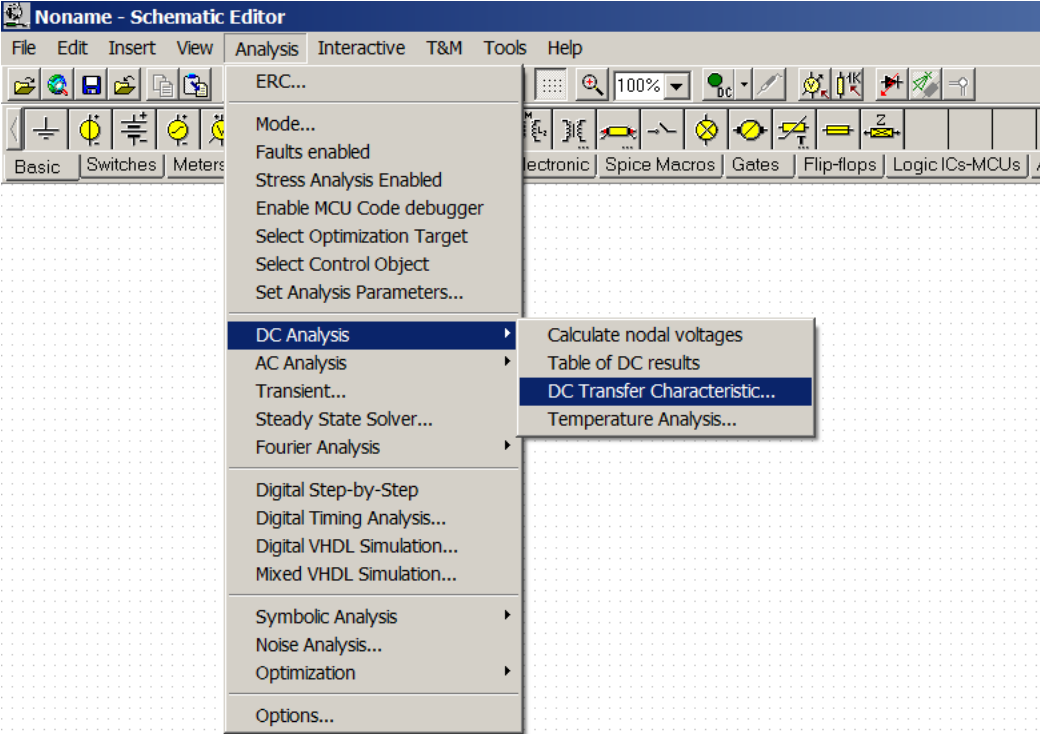
$$G_{diff} = 2 \cdot \left( \frac{2k\Omega}{100k\Omega} \right) = 0.04$$

$$V_{out} = G_{diff} \cdot V_{in}$$

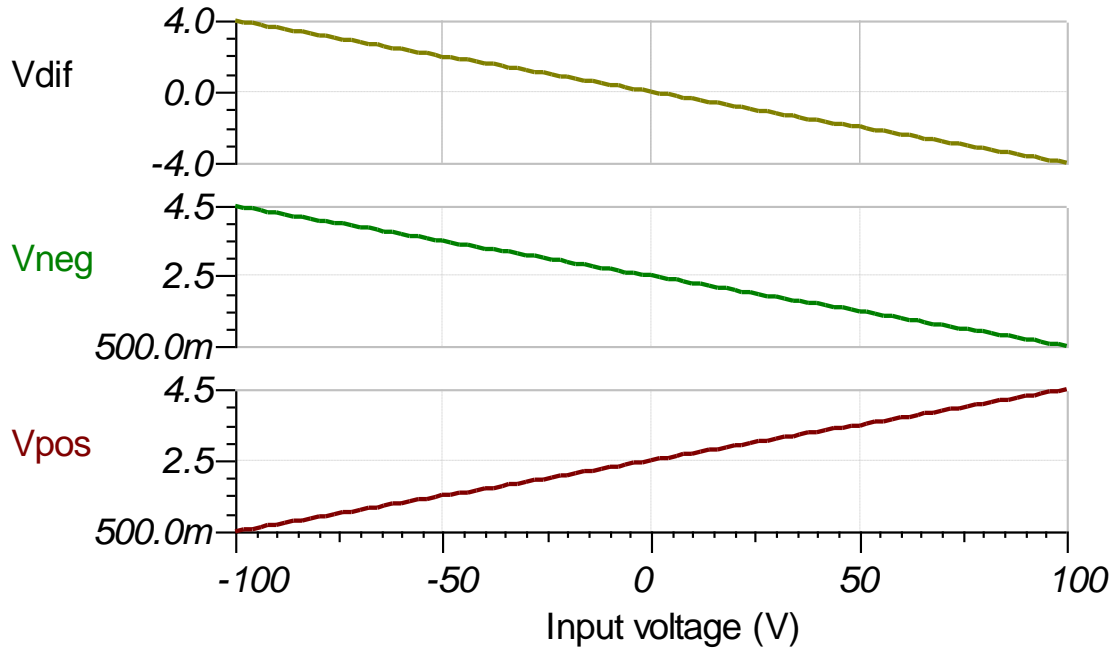
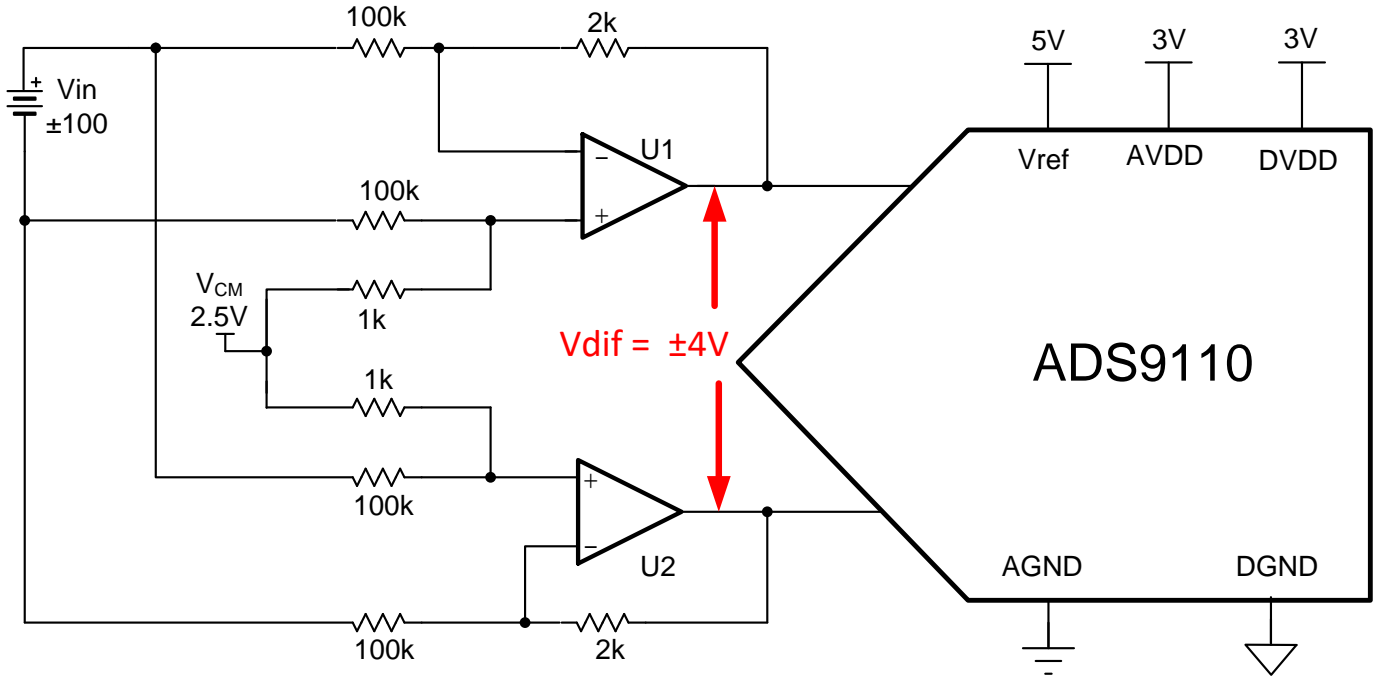
$$V_{out} = (0.04) \cdot (\pm 100V) = \pm 4V$$



# DC Transfer Function

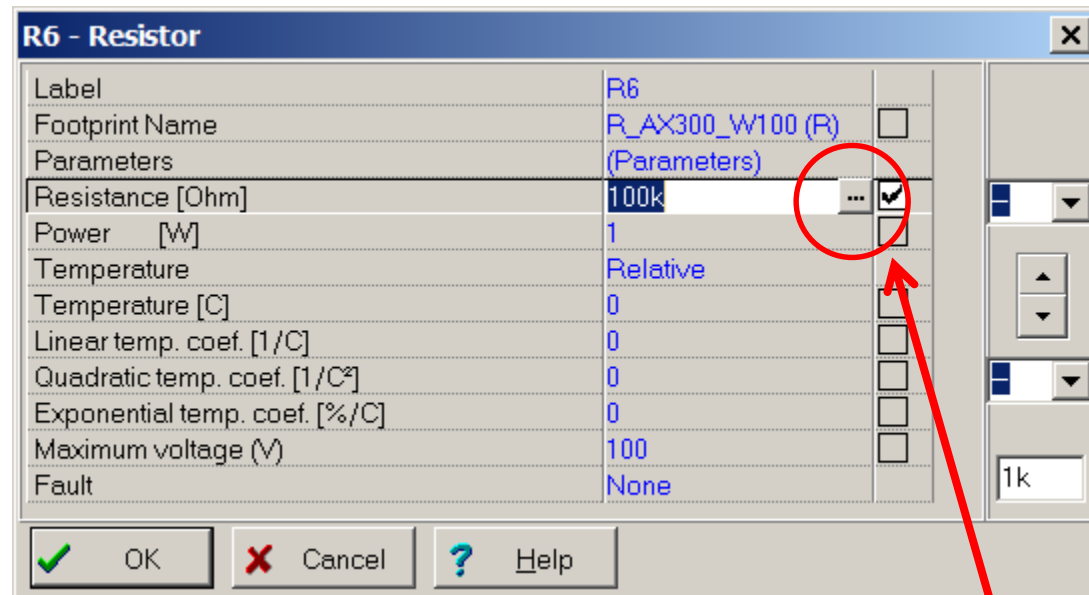


Select "Vin" for the input and enter the range from "Start value" to "End value"

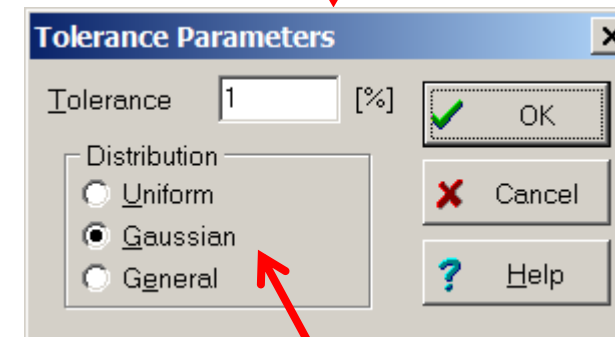


# Set tolerance on resistors and capacitors

Set to 1% or 0.1% per resistor spec

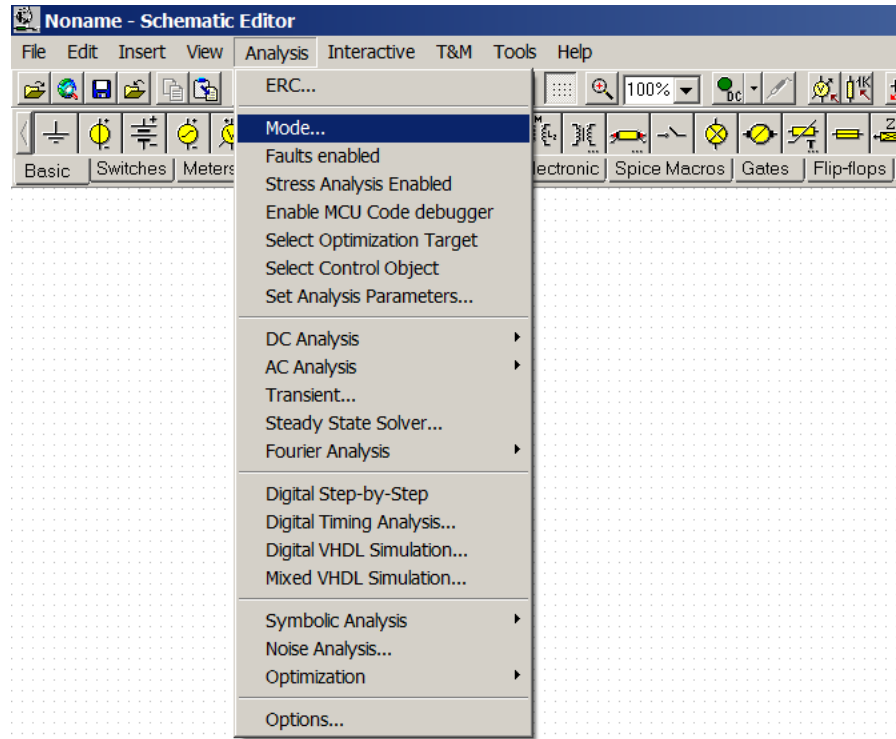


Click here to set the tolerance.

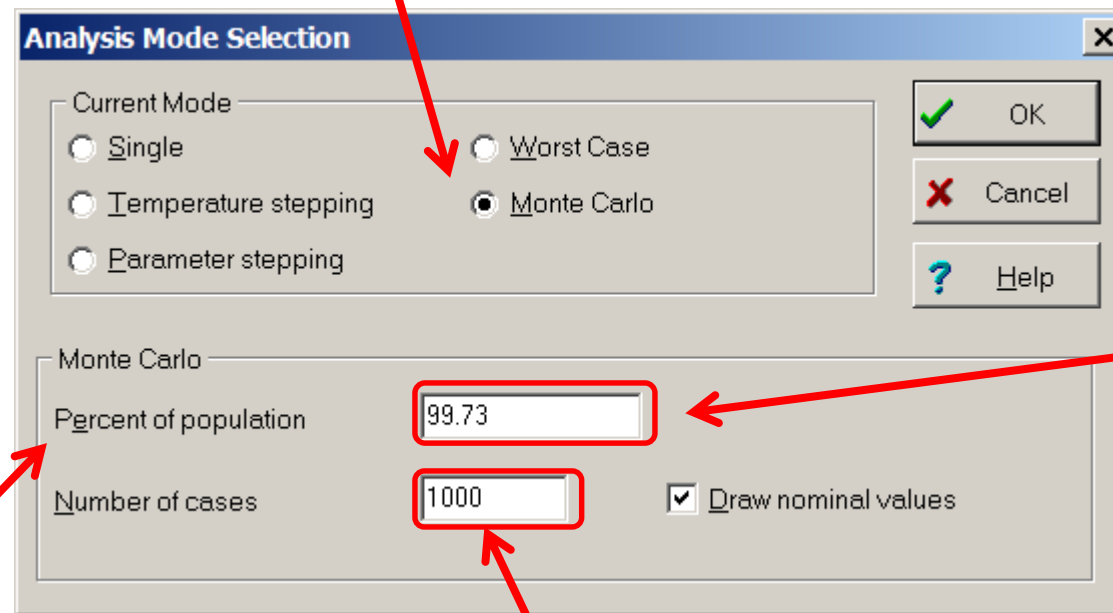


Gaussian Distribution

# Monte Carlo Analysis



Select "Monte Carlo"

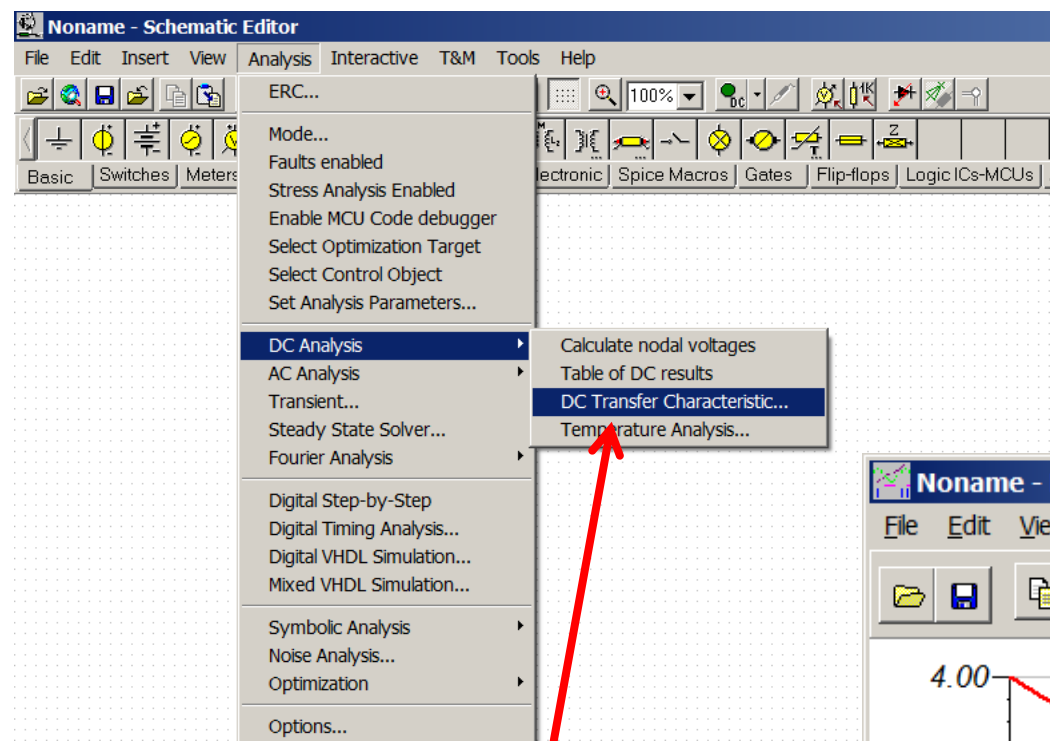


99.73% sets the component tolerance to  $\pm 3$  Standard deviations

Note the default of 68.26% will *not* give realistic results for resistor and capacitor tolerance.

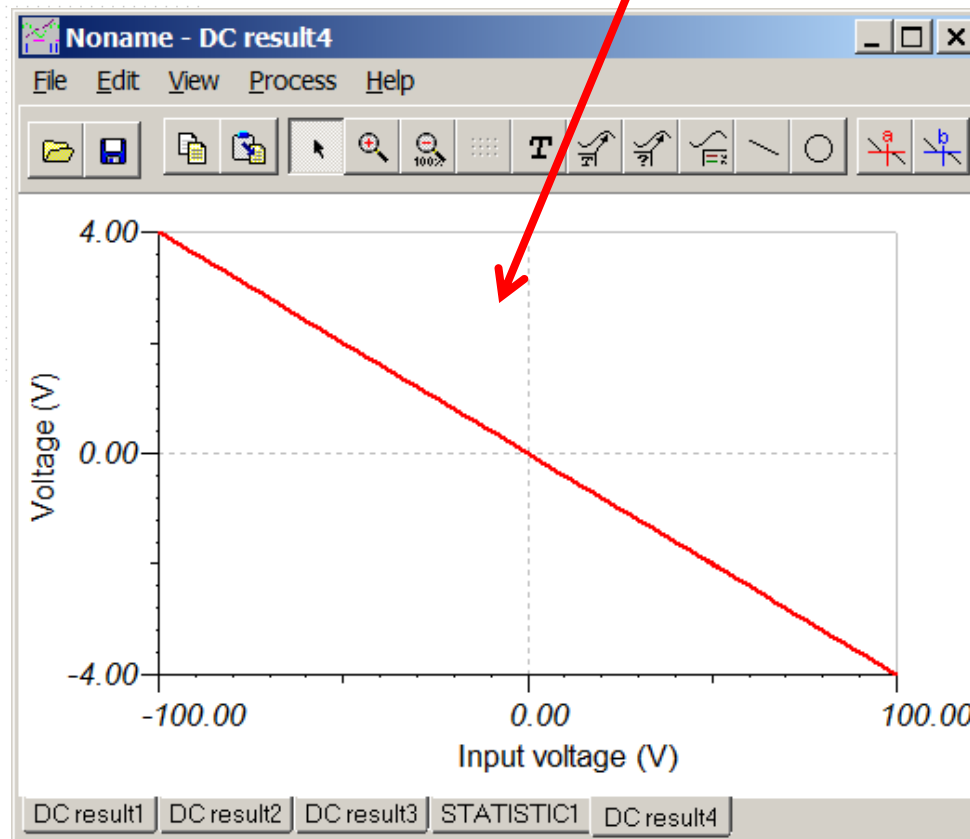
More cases will give you a better statistical distribution. The max is 1000.

# Monte Carlo for DC Transfer Characteristic

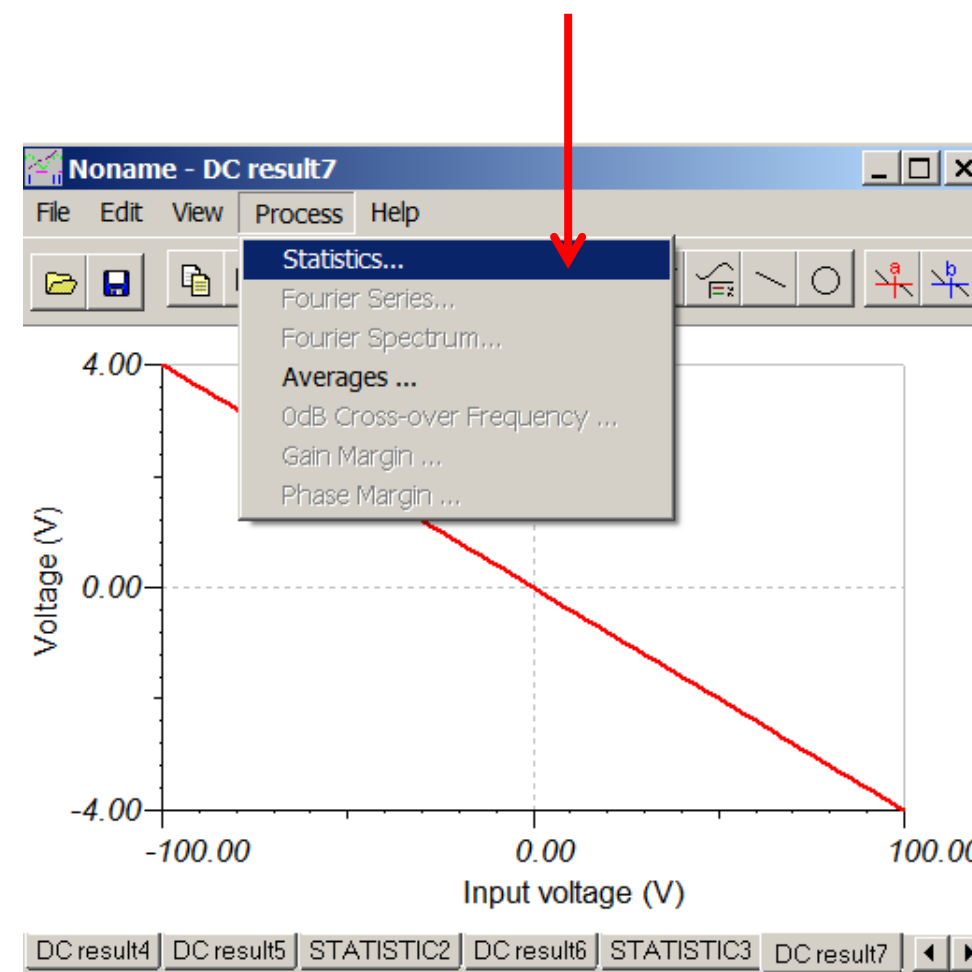


1. Run a dc transfer characteristic

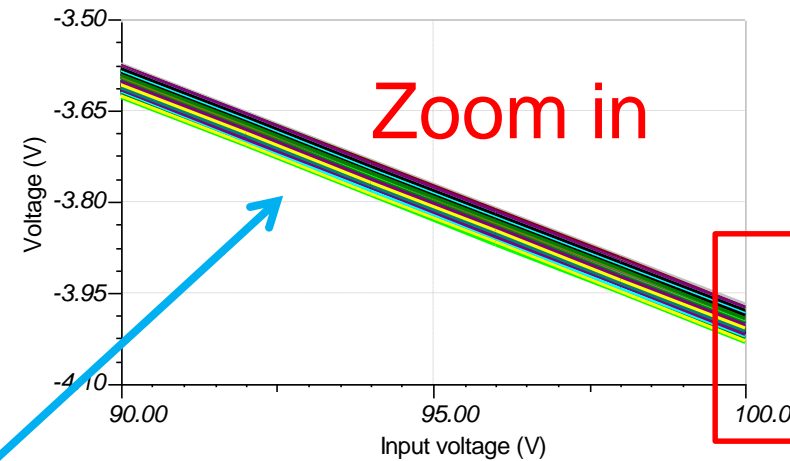
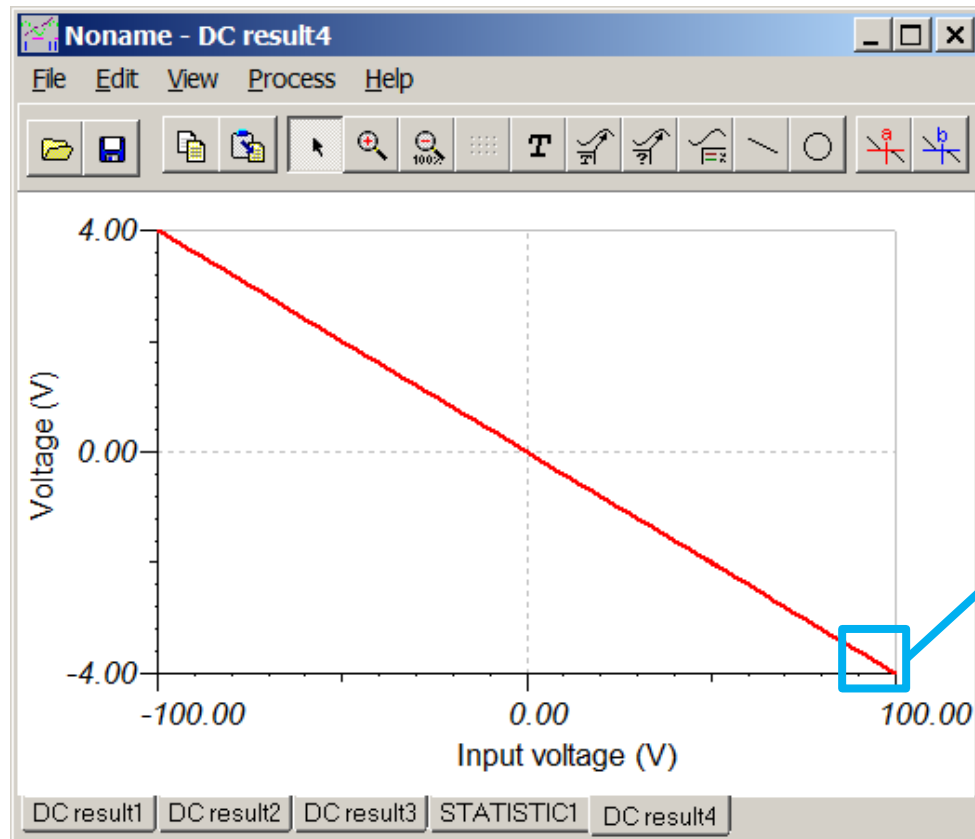
2. Press CTRL+Alt to select all



3. Select Process>Statistics



# The cut option



We generate the distribution from the vertical section at  $x=100$

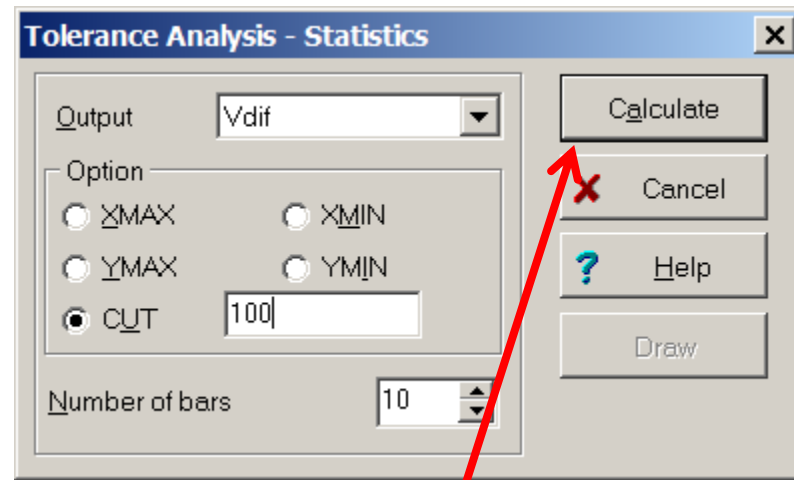
Tolerance Analysis - Statistics  
Output Vdif  
Option  
 XMAX  XMIN  
 YMAX  YMIN  
 CUT 100  
Number of bars 10  
Calculate  
Cancel  
Help  
Draw

Use Cut option

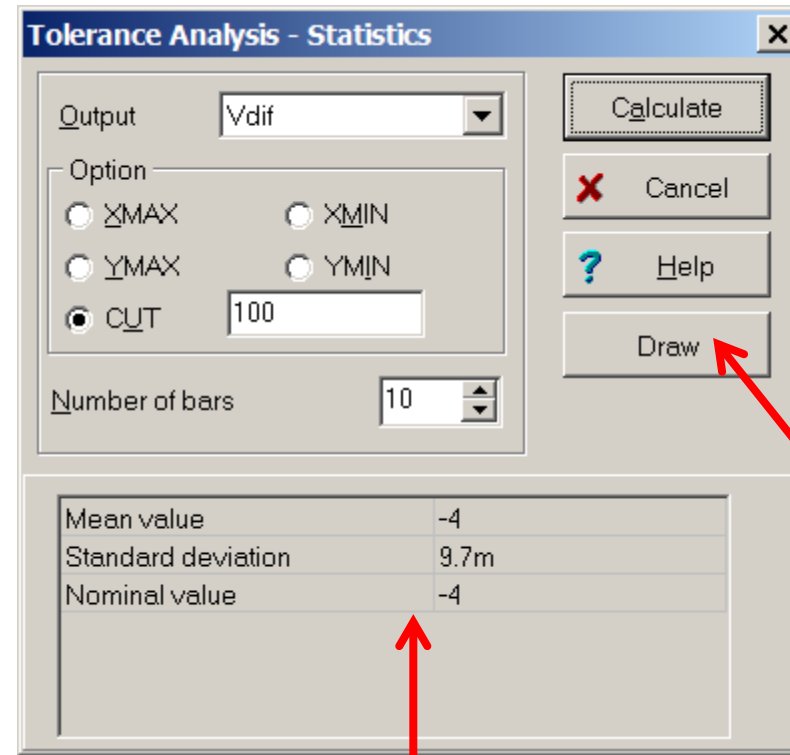
Enter the X-axis value where the cut set is taken

Number of bins in histogram. 10 is usually sufficient

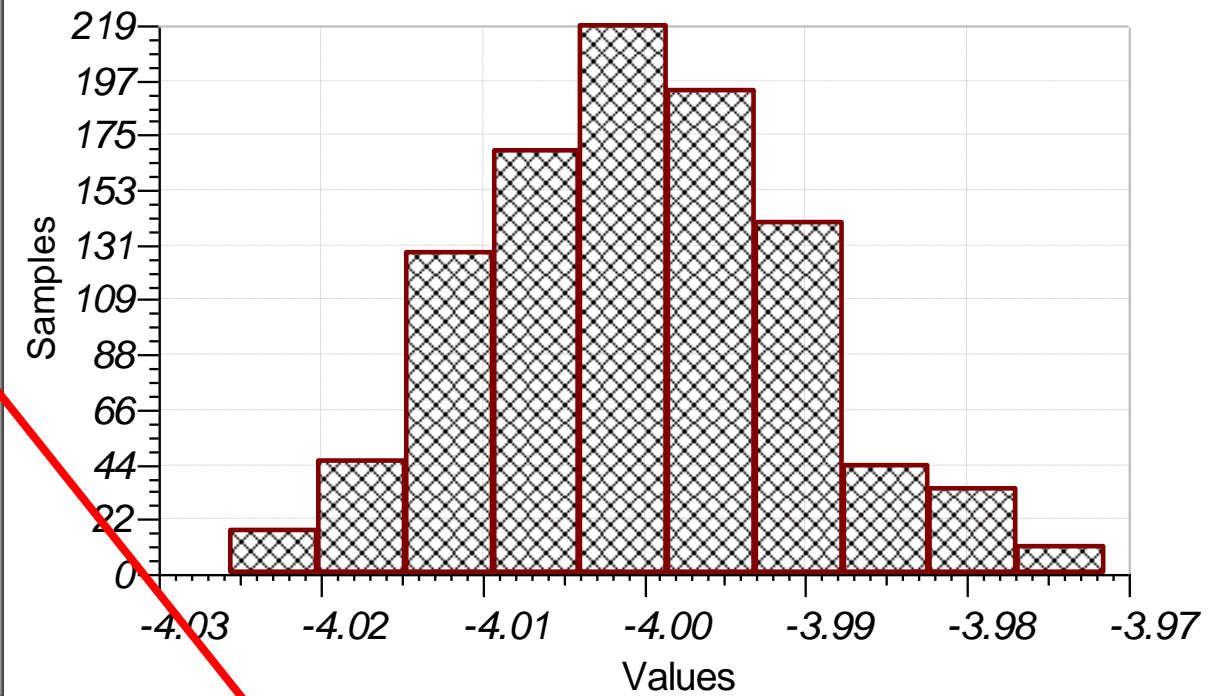
# Generate the statistical data and histogram



Press Calculate to get statistics, and draw to show histogram



Use to calculate gain error.



Press draw to get a graph of the histogram

$$TypGainError = \frac{\text{standard deviation}}{\text{Mean}} \cdot 100 = \left( \frac{9.7m}{4} \right) \cdot 100 = \pm 0.24\%$$

For 68.26% of the population

$$MaxGainError = 3 \cdot Typical = 3 \cdot (\pm 0.24\%) = 0.73\%$$

For 99.73% of the population



**Thanks for your time!**  
**Please try the quiz.**

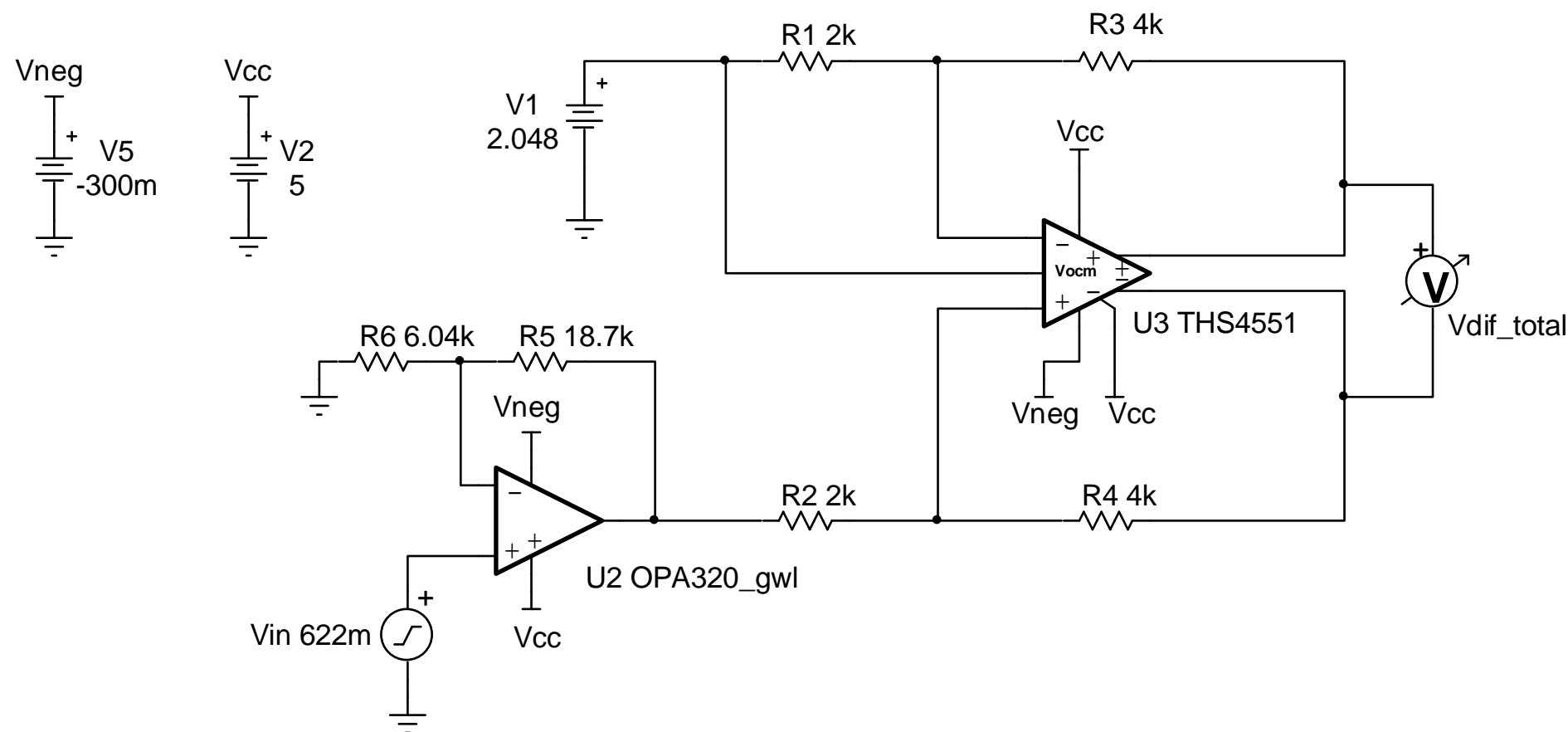
# Quiz: Using SPICE Monte Carlo Tool for Statistical Error Analysis

TIPL 4203  
TI Precision Labs – ADCs

Created by Art Kay

# Quiz: SPICE Monte Carlo Tool

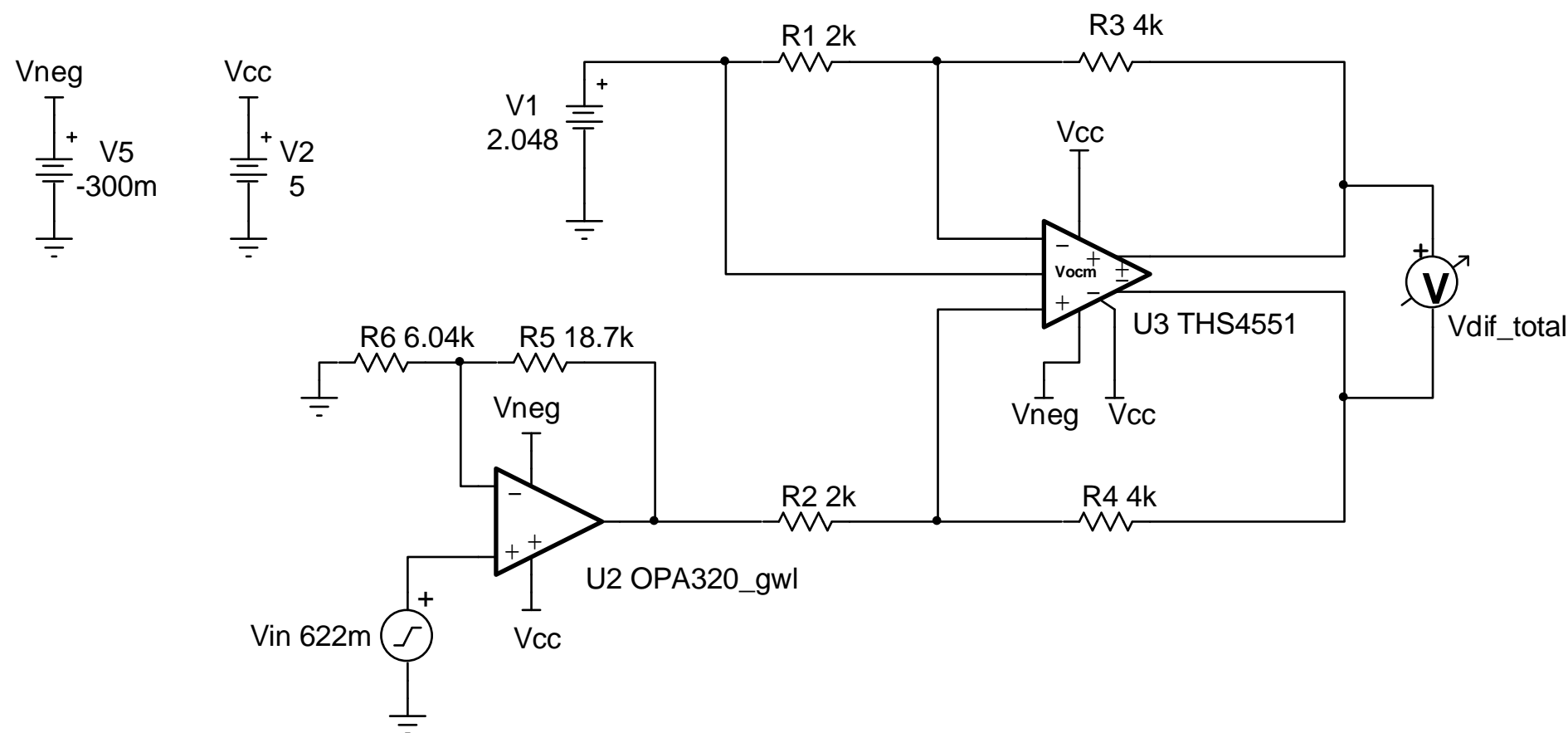
1. Use Monte Carlo analysis to determine a statistical estimate of typical and worst case gain error. Assume each resistor has a  $\pm 0.1\%$  tolerance. Note: this exercise assumes that you are using the "Industrial" version of TINA SPICE. TINA-TI does not include this feature. Many other SPICE simulators also include Monte Carlo capabilities, so you should get similar results if you are using another simulator.



# Solutions

# Quiz: SPICE Monte Carlo Tool

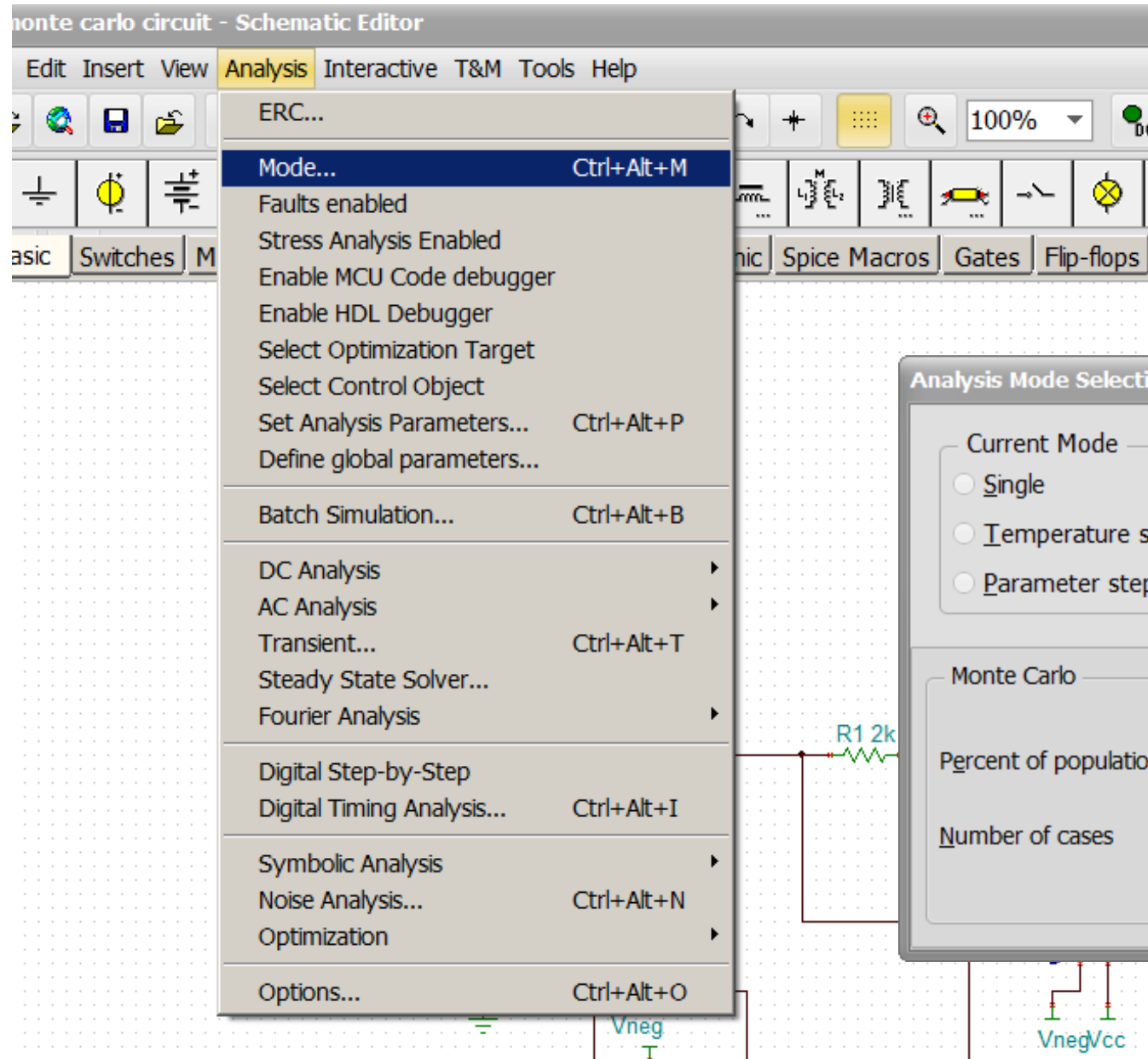
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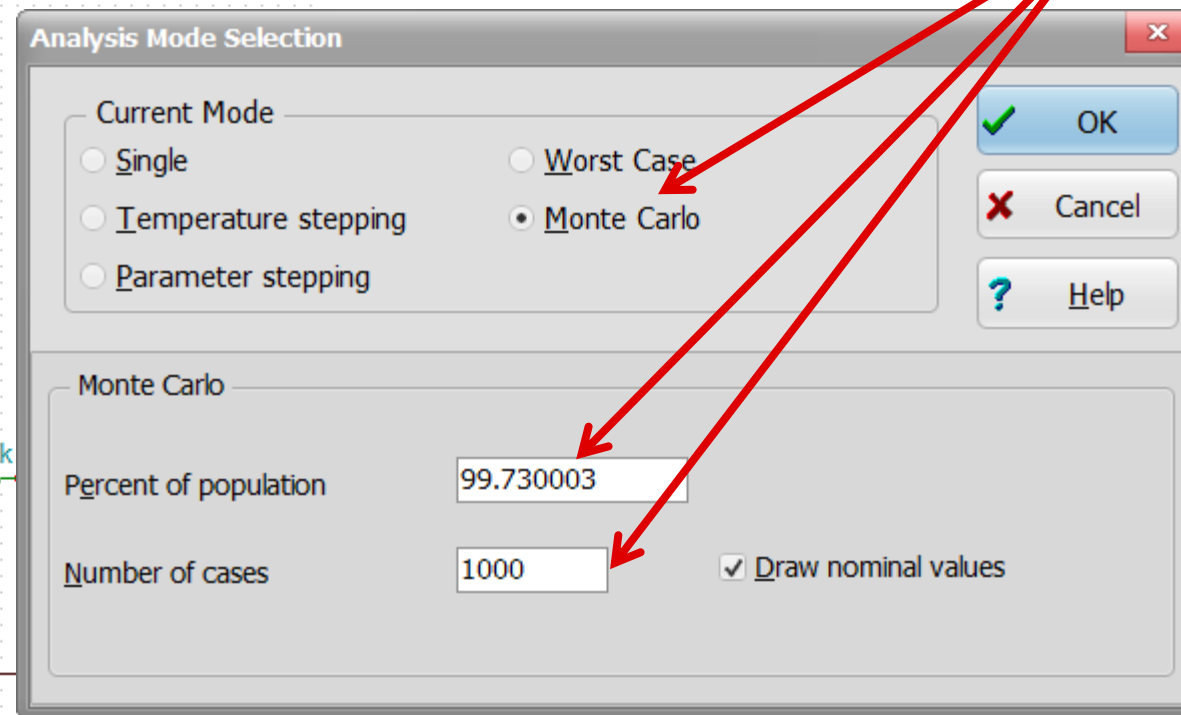
Click on this imbedded file, for the TINA spice file used in this solution.



# Quiz: SPICE Monte Carlo Tool



1. Set Monte Carlo Mode
2. Set percent of population to 99.73%
3. Set Number of cases to 1000



# Quiz: SPICE Monte Carlo Tool

1. Update the tolerance of each resistor by clicking on the component.
2. Press the button next to the resistance.
3. Enter the tolerance (0.1% in this case)
4. Select Gaussian distribution.

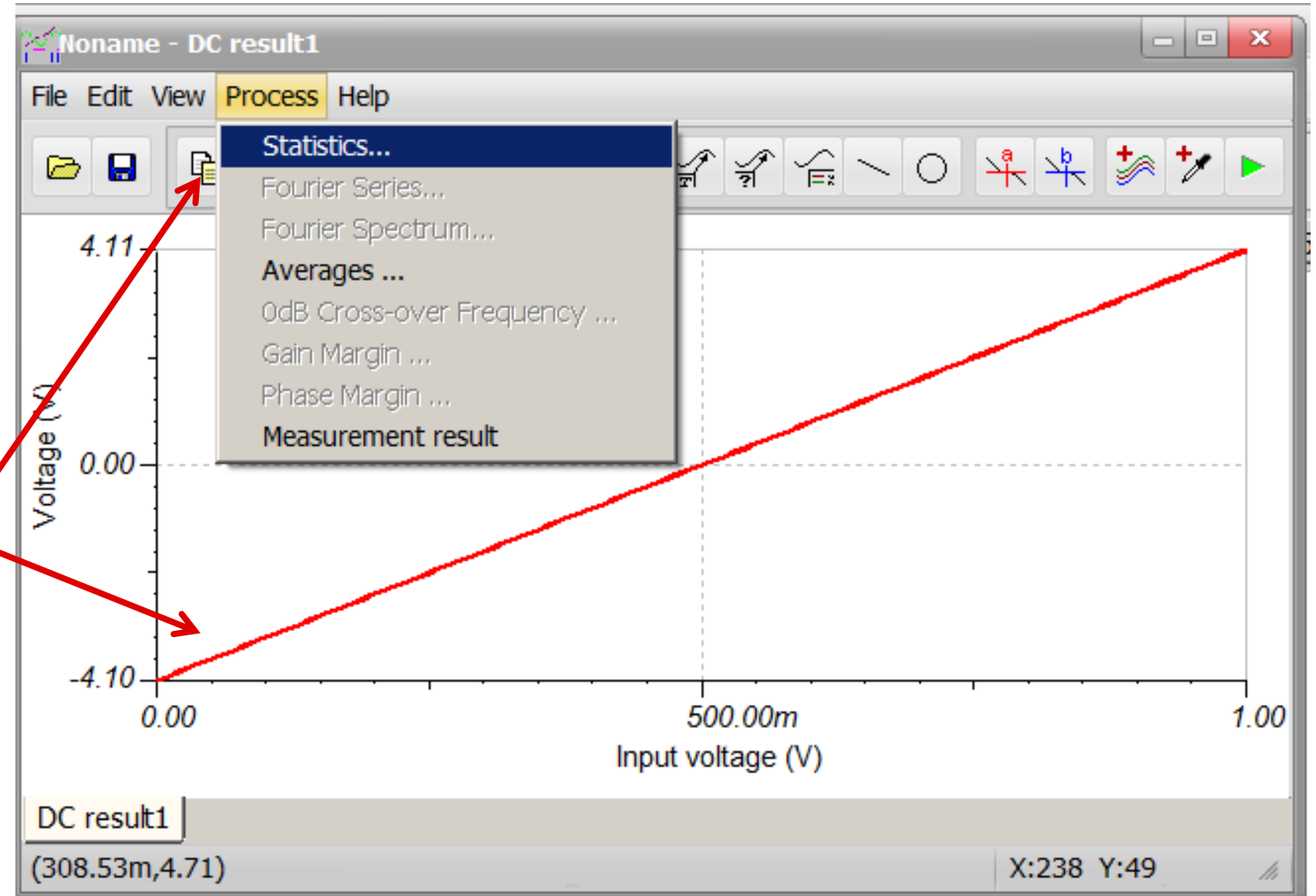
The image shows a SPICE simulation tool interface. On the left, a circuit diagram is visible with resistors R1 (2k), R2 (2k), R3 (4k), and R4 (4k), and an op-amp U3 (THS4551). The op-amp is powered by Vcc and Vneg/Vcc. A dialog box titled 'R3 - Resistor' is open, showing the following parameters:

Parameter	Value	Unit	Checkbox
Label	R3		
Footprint Name	R_AX600_W200 (R)		<input type="checkbox"/>
Parameters	(Parameters)		
Resistance [Ohm]	4k		<input checked="" type="checkbox"/>
Power [W]	1		<input type="checkbox"/>
Temperature	Relative		<input type="checkbox"/>
Temperature [C]	0		<input type="checkbox"/>
Linear temp. coef. [1/C]	0		<input type="checkbox"/>
Quadratic temp. coef. [1/C <sup>2</sup> ]	0		<input type="checkbox"/>
Exponential temp. coef. [%/C]	0		<input type="checkbox"/>
Maximum voltage (V)	100		<input type="checkbox"/>
Fault	None		<input type="checkbox"/>

Below the 'R3 - Resistor' dialog box, a 'Tolerance Parameters' dialog box is open, showing a tolerance of 0.1 [%] and the Gaussian distribution selected. The 'OK' button is highlighted.

# Quiz: SPICE Monte Carlo Tool

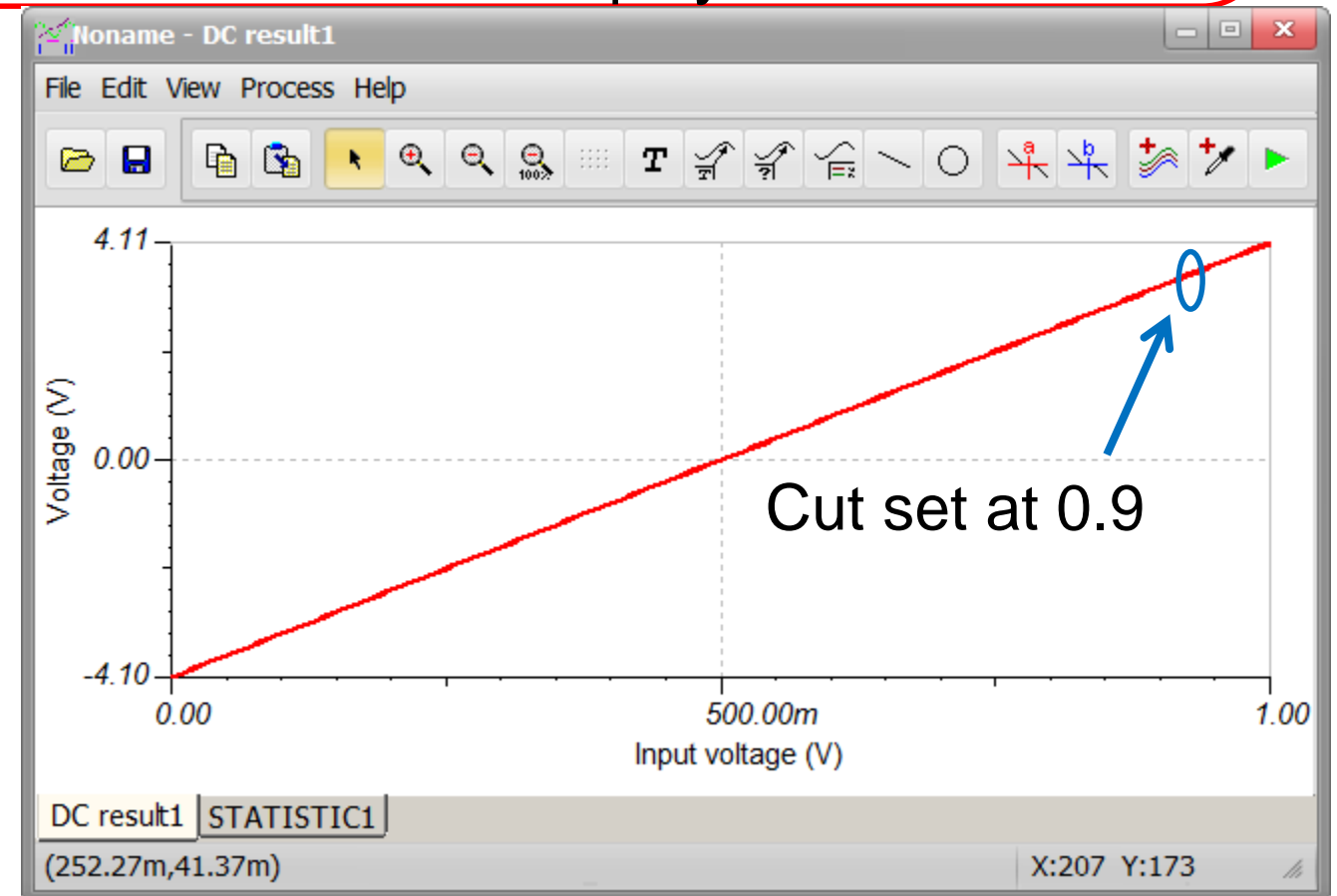
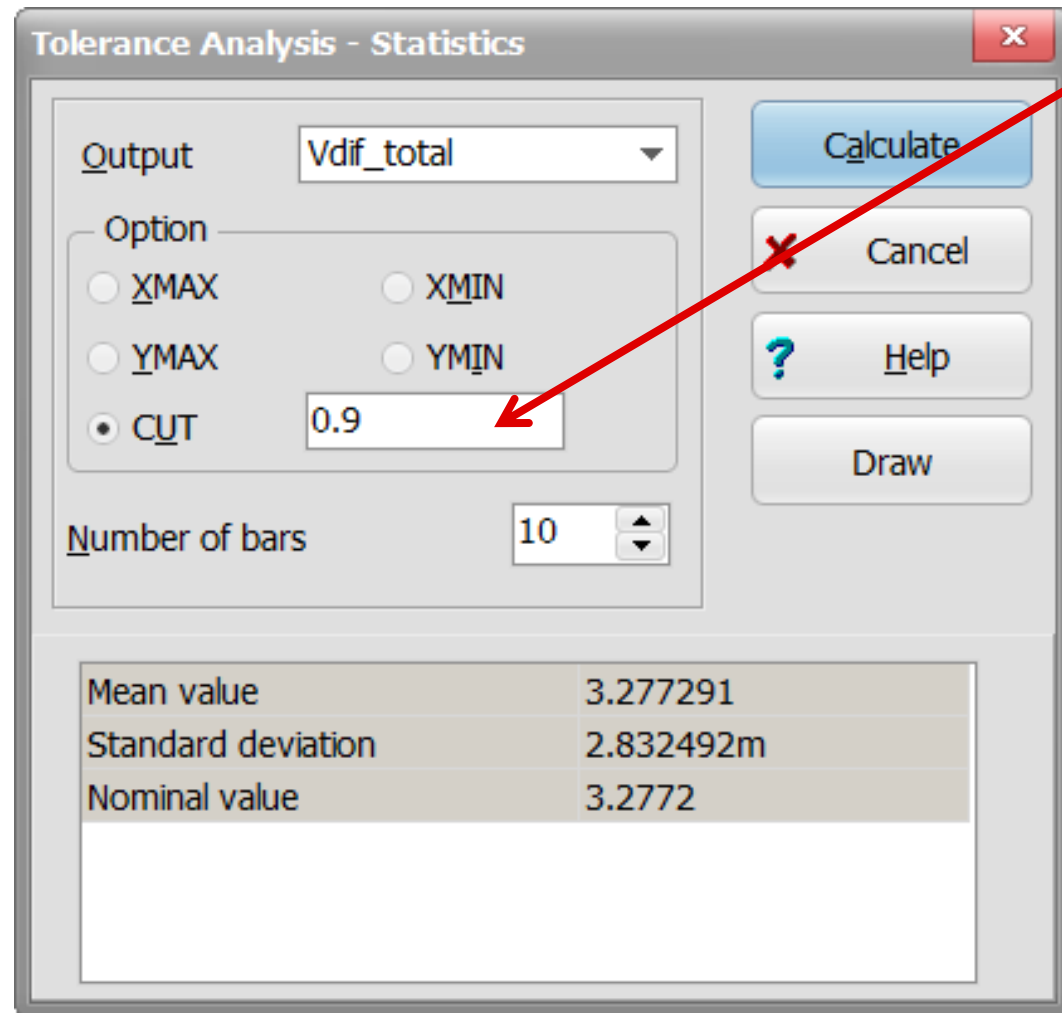
1. Click on graph and press "Ctrl+A" to select all the curves. It will highlight red when selected.
2. Select "Process>Statistics"





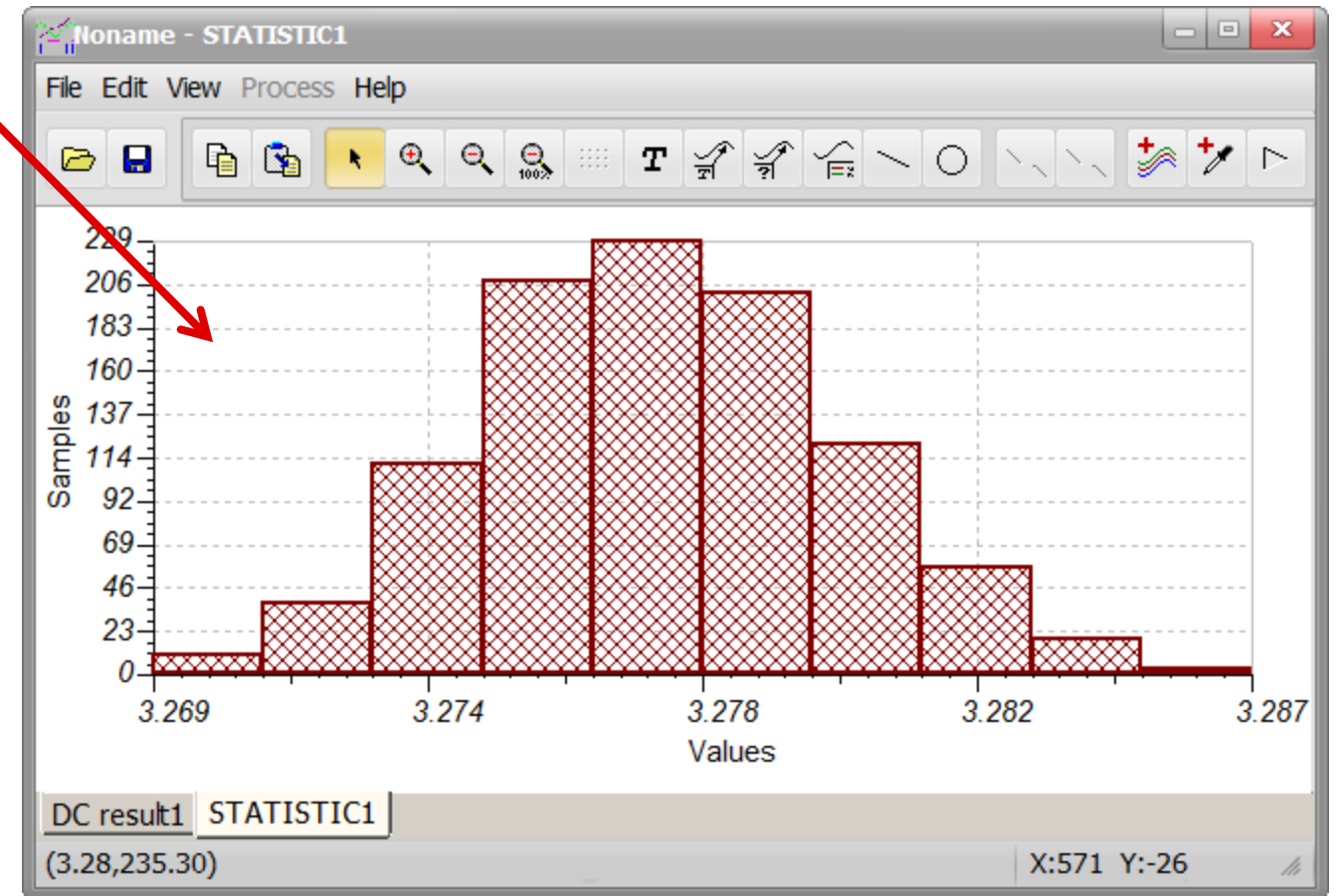
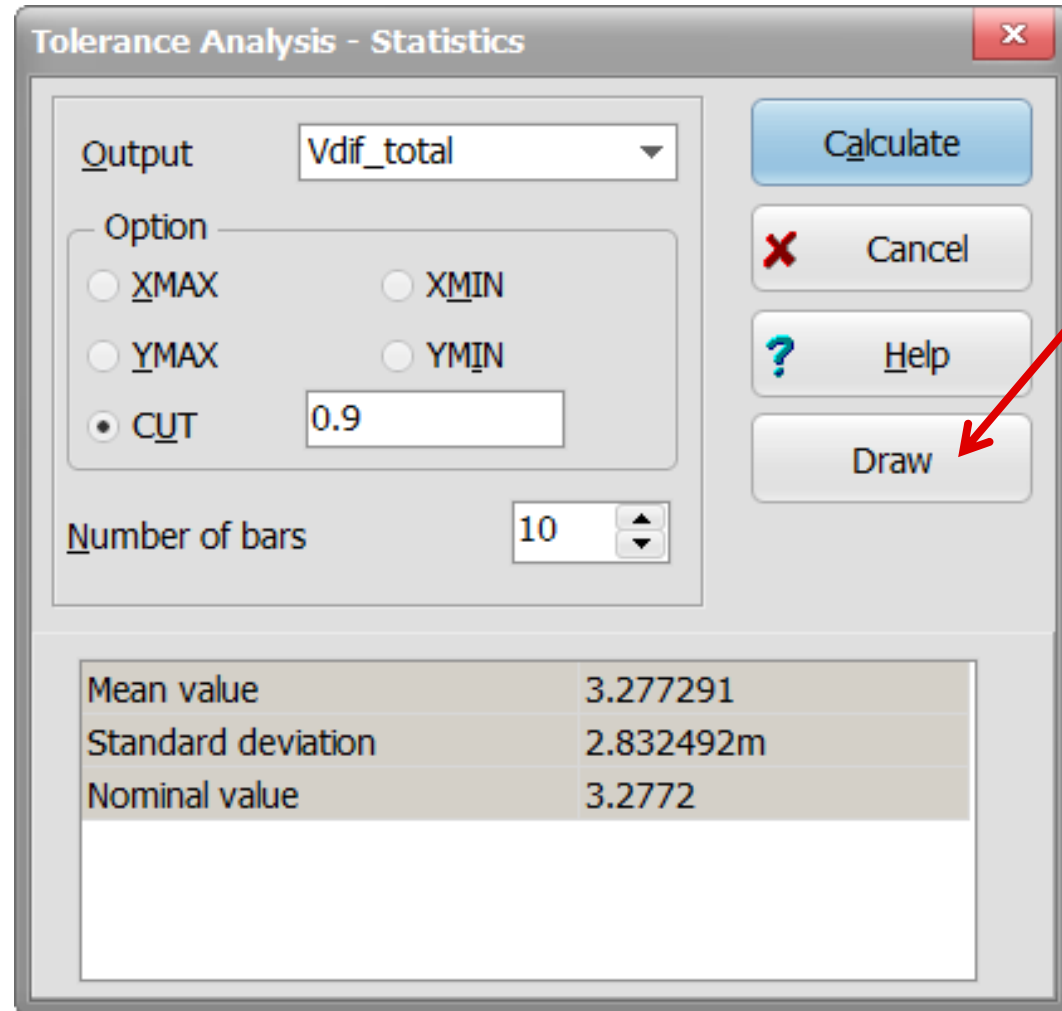
# Quiz: SPICE Monte Carlo Tool

1. Select "Cut" for a cut set of the curves. Enter a value for the cut set. In this case 0.9 is used to avoid the end points of the curve which may have non-linearity.
2. Press "Calculate". This will display the statistics.

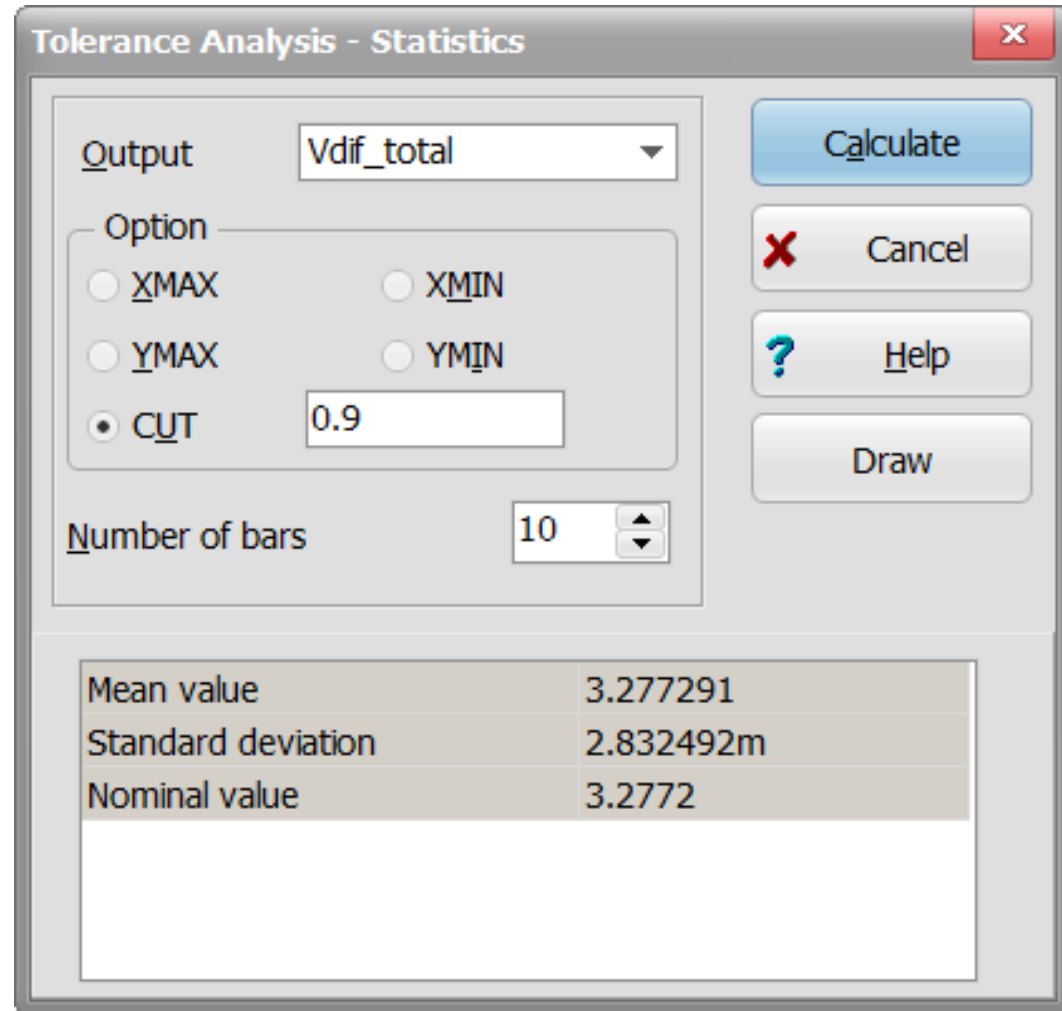


# Quiz: SPICE Monte Carlo Tool

1. Press "Draw" to show the histogram.



# Quiz: SPICE Monte Carlo Tool



$$\text{TypicalGainError} = \frac{\text{StandardDeviation}}{\text{NominalValue}} \cdot 100$$

$$\text{TypicalGainError} = \frac{3.83\text{mV}}{3.2777\text{V}} \cdot 100 = \pm 0.11\%$$

$$\text{MaximumGainError} = \text{TypicalGainError} \cdot 3 = \pm 0.33\%$$

Note: Typical gain error represents one standard deviation of gain error or 68.3% of the population. Maximum gain error represents  $\pm 3$  standard deviations or 99.73