

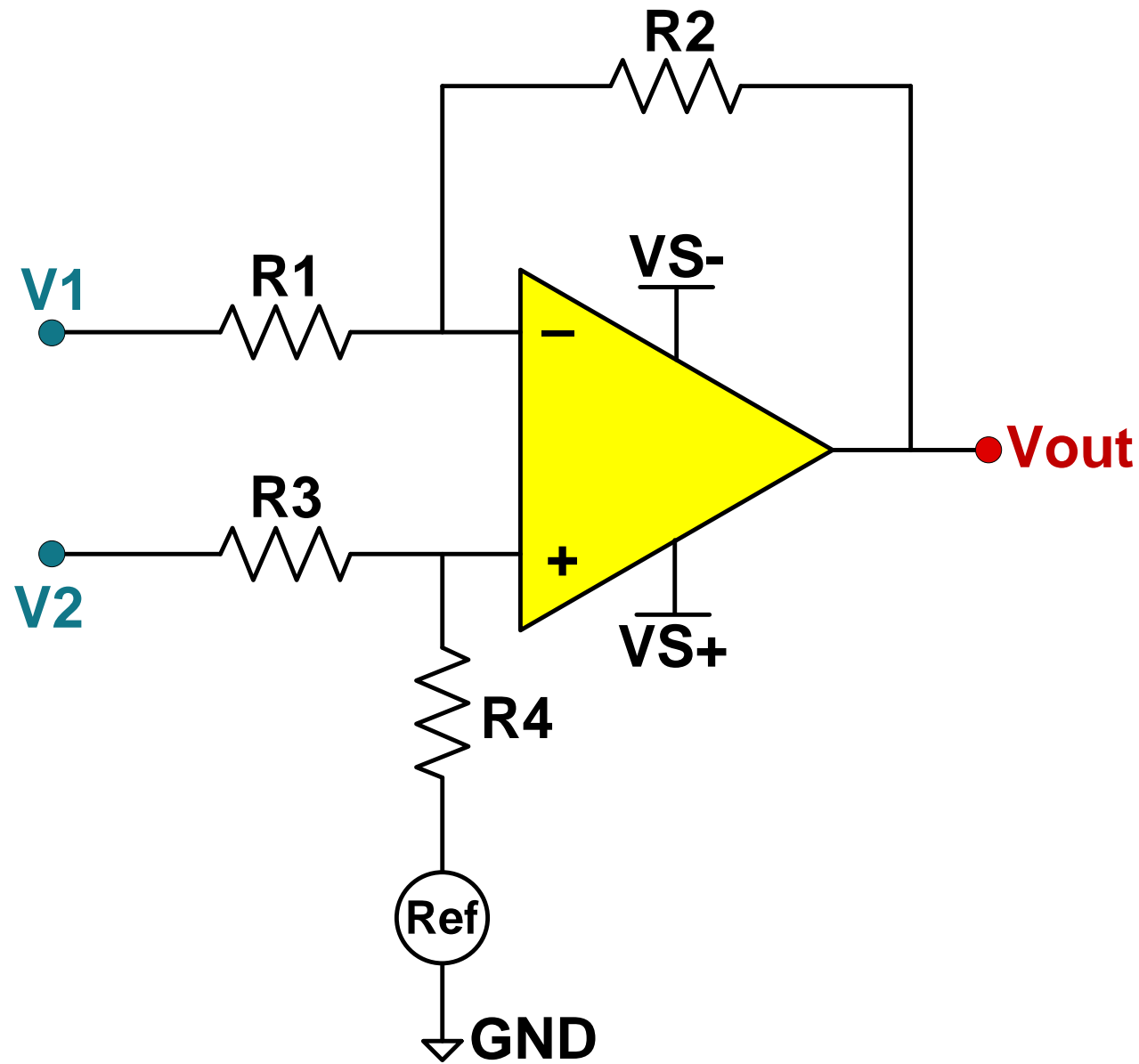
# Instrumentation Amplifier (IA) topologies: two-amp

TI Precision Labs – Instrumentation Amplifiers

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Prepared by Tamara Alani

# IA topologies – One amp recap



**Difference amplifier output equation:**

$$V_{out} = V_d \times A_d + Ref$$

Where  $A_d$  is the gain of the circuit

If  $R_1 = R_3$ , and  $R_2 = R_4$ , then  $A_d = \frac{R_2}{R_1}$

**Challenges:**

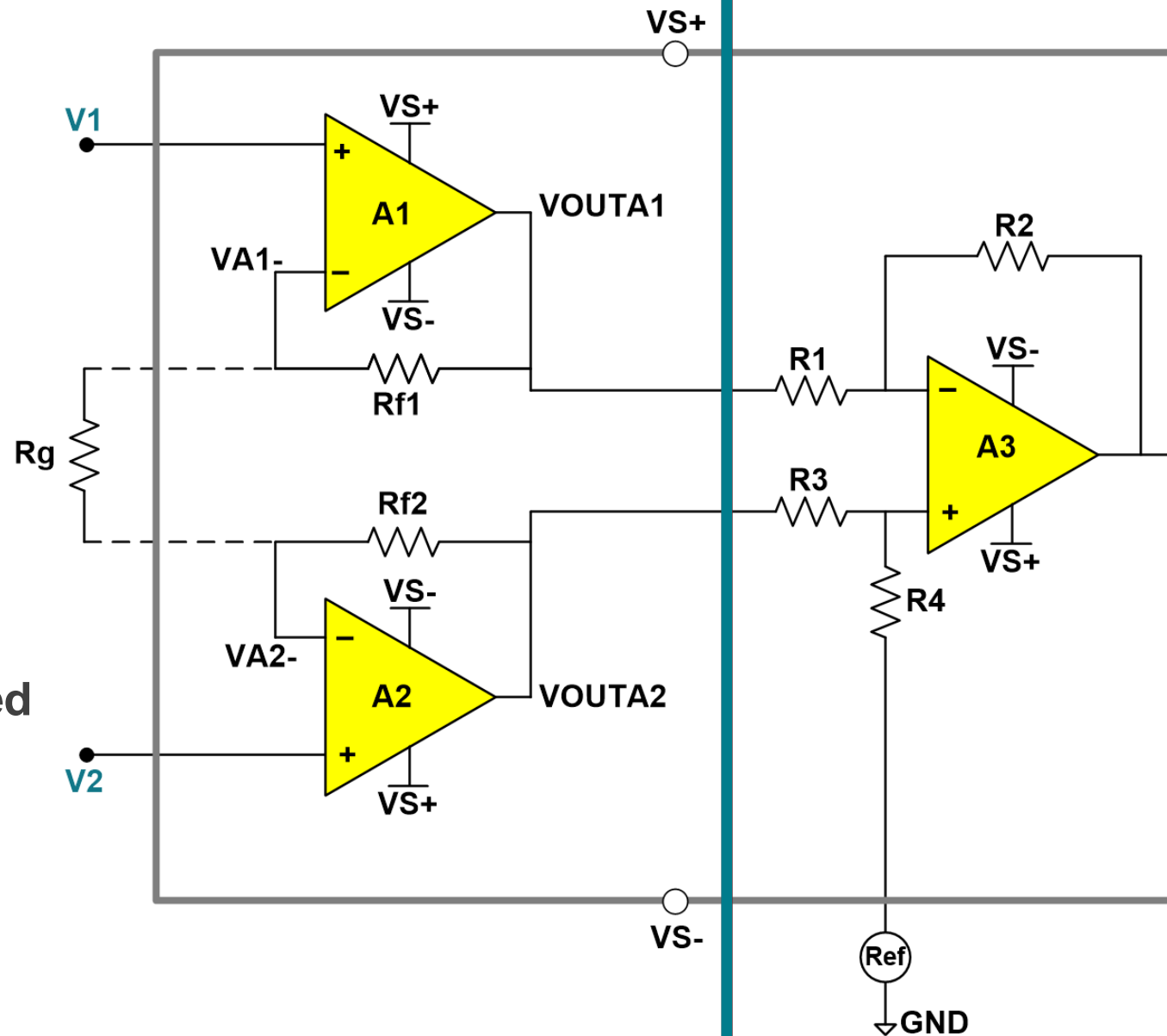
1. Precision relies on matched resistors
2. Low input impedance

# IA topologies – Three amp recap

Buffer stage with gain and high input impedance

Rf1 and Rf2 are absolutely matched for precise gain calculation:

$$A_d = 1 + \frac{2R_f}{R_g}$$



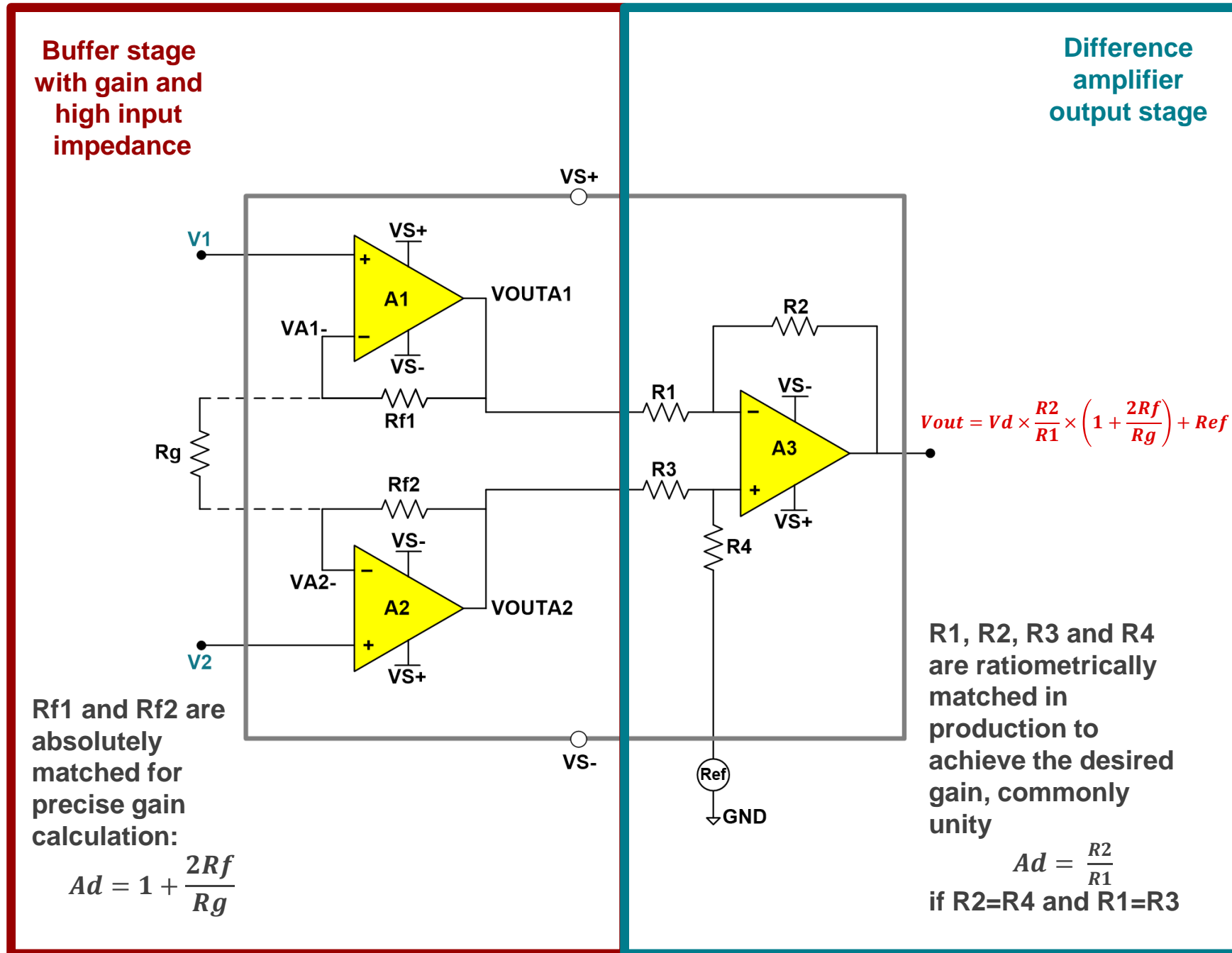
Difference amplifier output stage

$$V_{out} = V_d \times \frac{R_2}{R_1} \times \left( 1 + \frac{2R_f}{R_g} \right) + Ref$$

R1, R2, R3 and R4 are ratiometrically matched in production to achieve the desired gain, commonly unity

$$A_d = \frac{R_2}{R_1} \text{ if } R_2=R_4 \text{ and } R_1=R_3$$

# IA topologies – Three amp recap cont'd



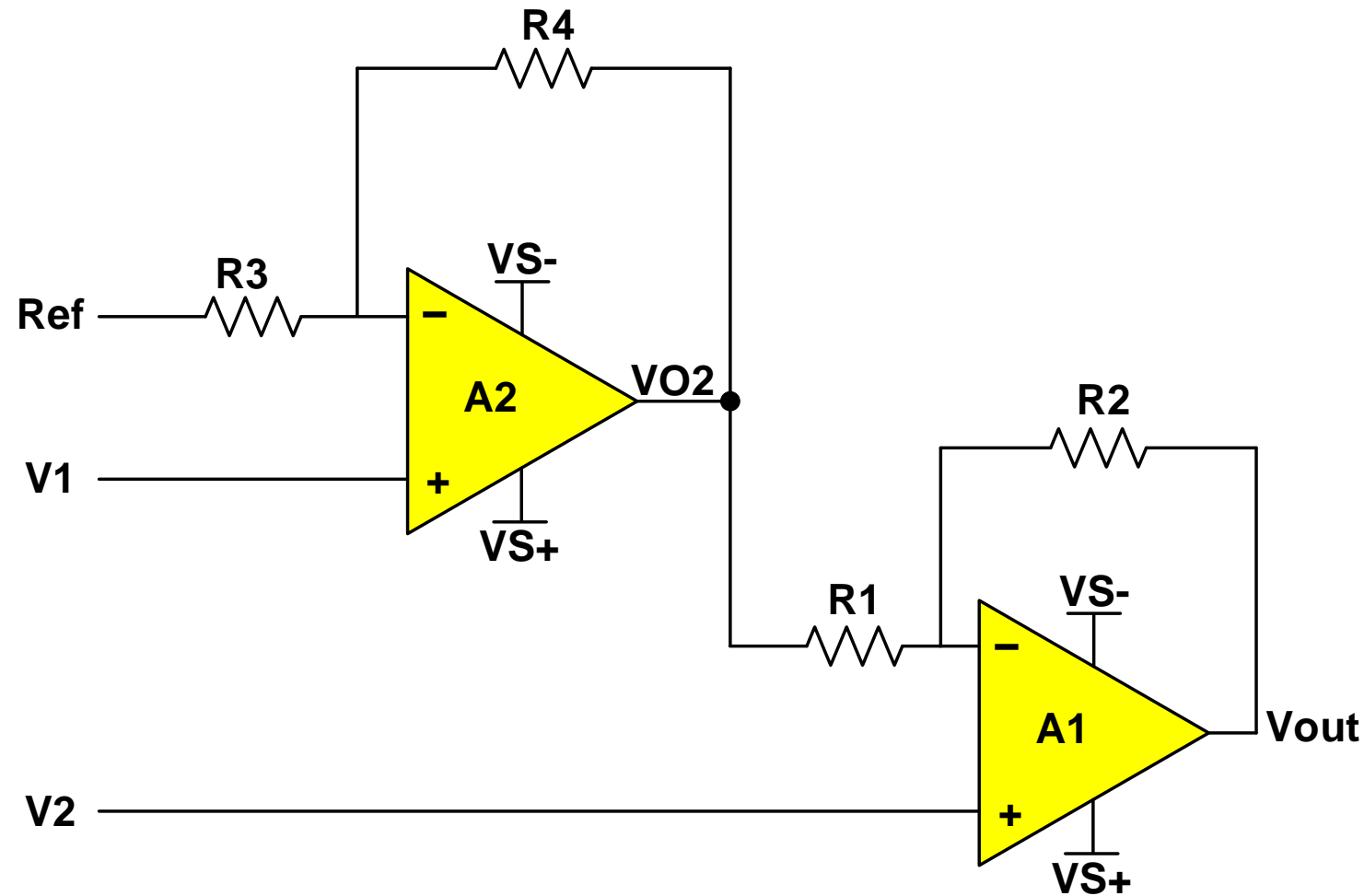
## Drawbacks:

Complex design: 3 amplifiers and 6 resistors.

This complexity may result in:

- larger die size,
- higher current consumption,
- higher manufacturing cost.

# IA topologies – Two amp IA introduction



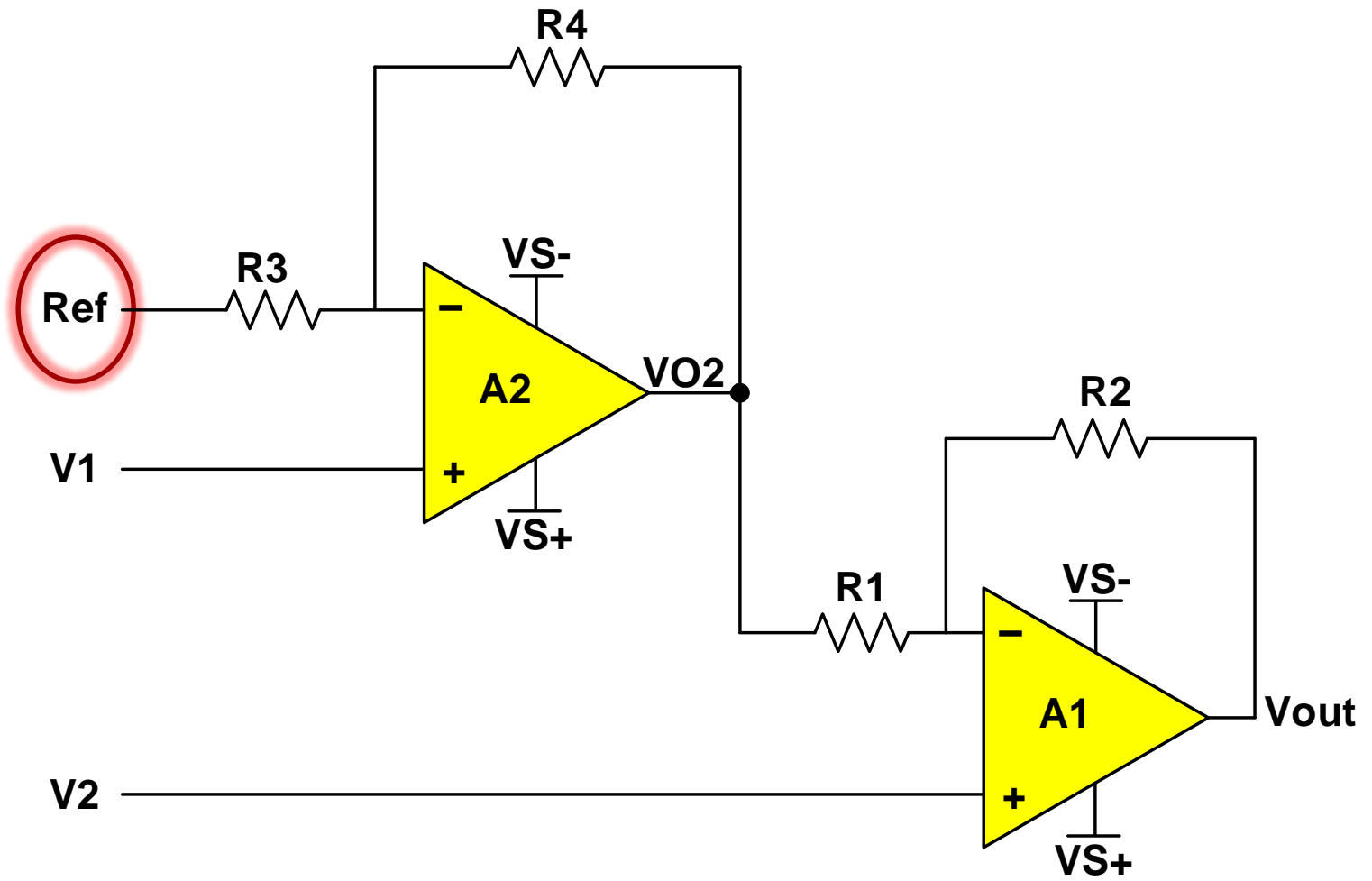
## Design simplicity:

- 2 amps, 4 resistors →
  - smaller IC
  - lower current consumption
  - smaller manufacturing cost

## Input impedance:

- High (typically  $10^9 \Omega$ )

# IA topologies – 2 amp IA derivation; A2 derivation



Derive output of A2 using superposition theorem:

Equation	V1	Ref
V1*	Keep	Short
Ref*	Short	Keep
<b><math>VO2 = V2^* + Ref^*</math></b>		

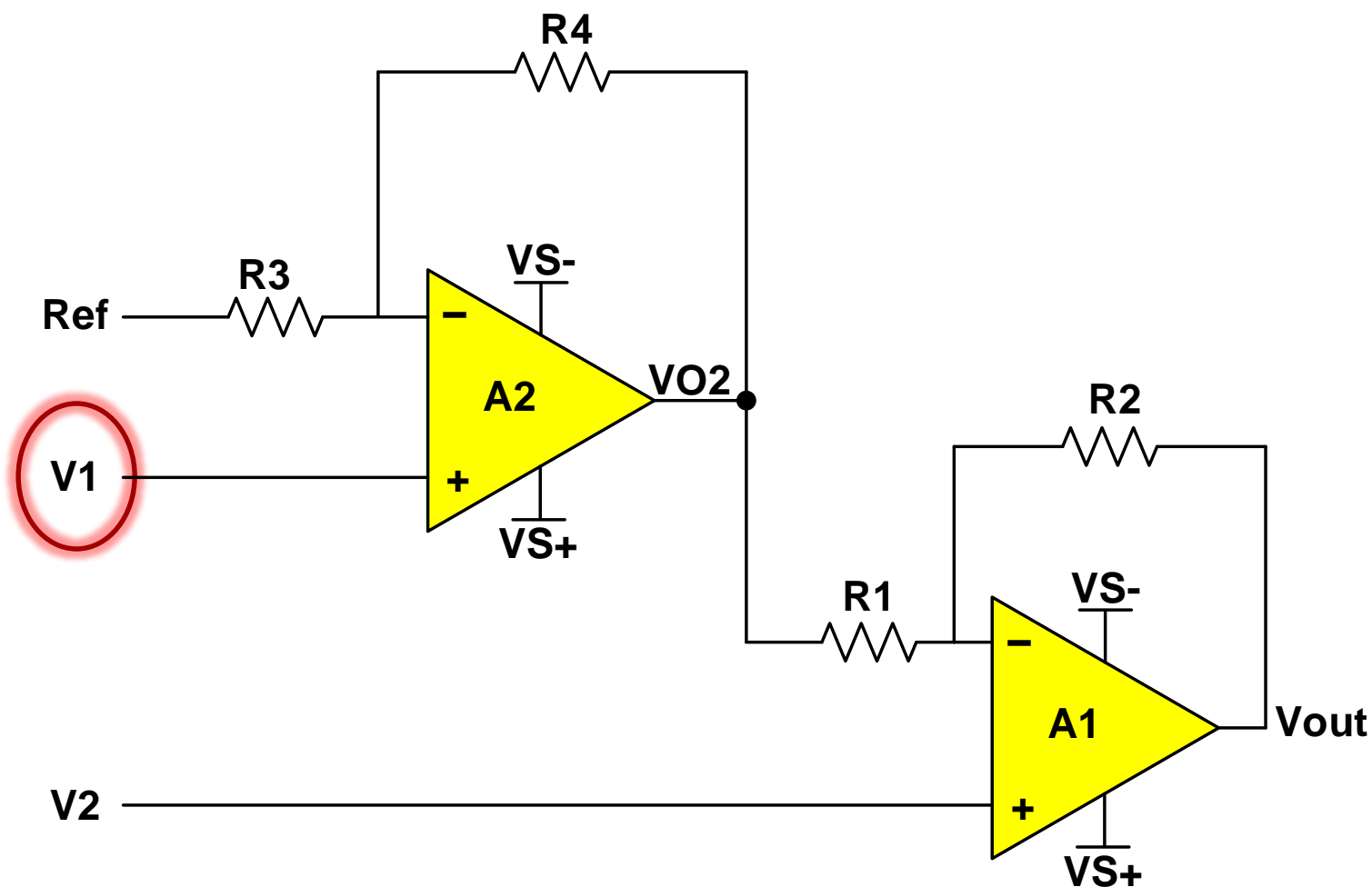
Ground Ref:

A2 looks like non-inverting configuration:

$$VO2 = \left( 1 + \frac{R4}{R3} \right) \times V1$$

Equation V1\*

# IA topologies – 2 amp IA derivation; A2 derivation



Derive output of A2 using superposition theorem:

Equation	V1	Ref
V1*	Keep	Short
Ref*	Short	Keep
<b><math>VO2 = V2^* + Ref^*</math></b>		

Ground V1:

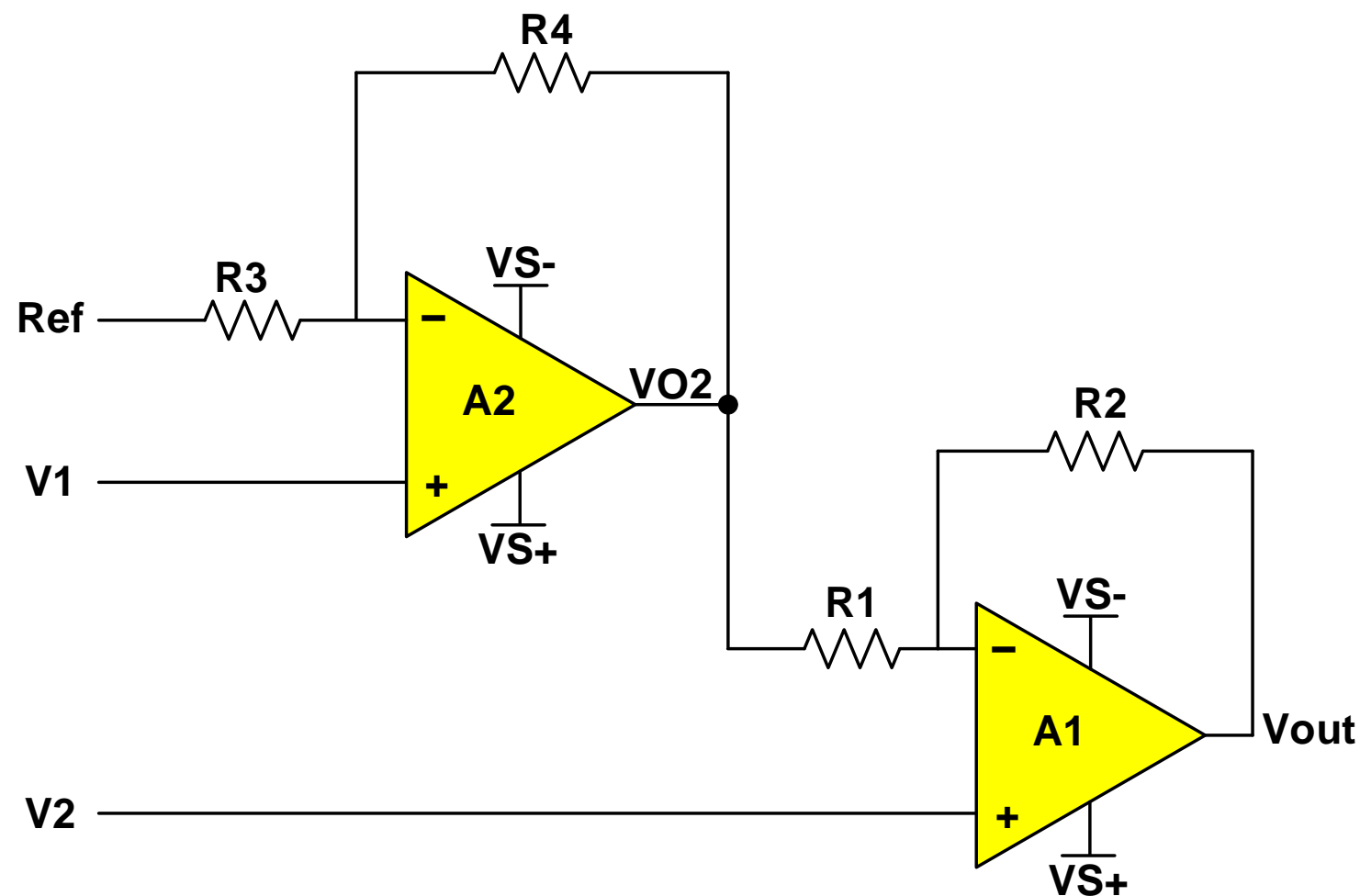
A2 looks like inverting configuration:

$$VO2 = \left( -\frac{R4}{R3} \right) \times Ref$$

Equation Ref\*

# IA topologies – 2 amp IA derivation; A2 derivation

Derive output of A2 using superposition theorem:



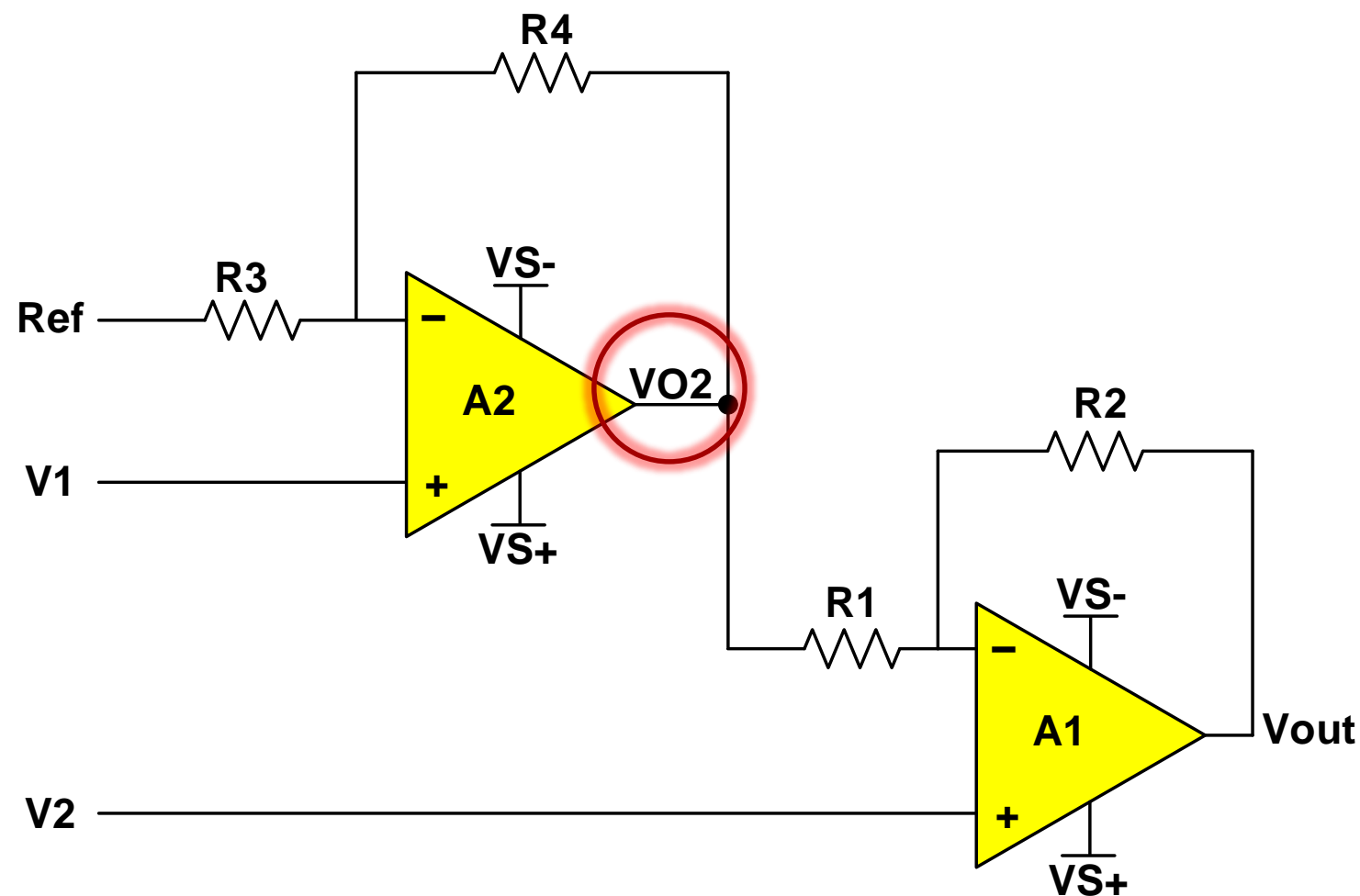
Equation	V1*	Ref	
V1*	Keep	Short	$V1^* = (1+R4/R3) \times V1$
Ref*	Short	Keep	$Ref^* = (-R4/R3) \times Ref$
<b><math>VO2 = V1^* + Ref^*</math></b>			

Combine equations  $V1^*$  and  $Ref^*$  to yield VO2:

$$VO2 = \frac{-R4}{R3} \times Ref + \left(1 + \frac{R4}{R3}\right) \times V1$$



# IA topologies – 2 amp IA derivation; A1 derivation



Derive output of A1 using superposition theorem:

Equation	V2	VO2
V2*	Keep	Short
VO2*	Short	Keep
<b><math>V_{out} = V2^* + VO2^*</math></b>		

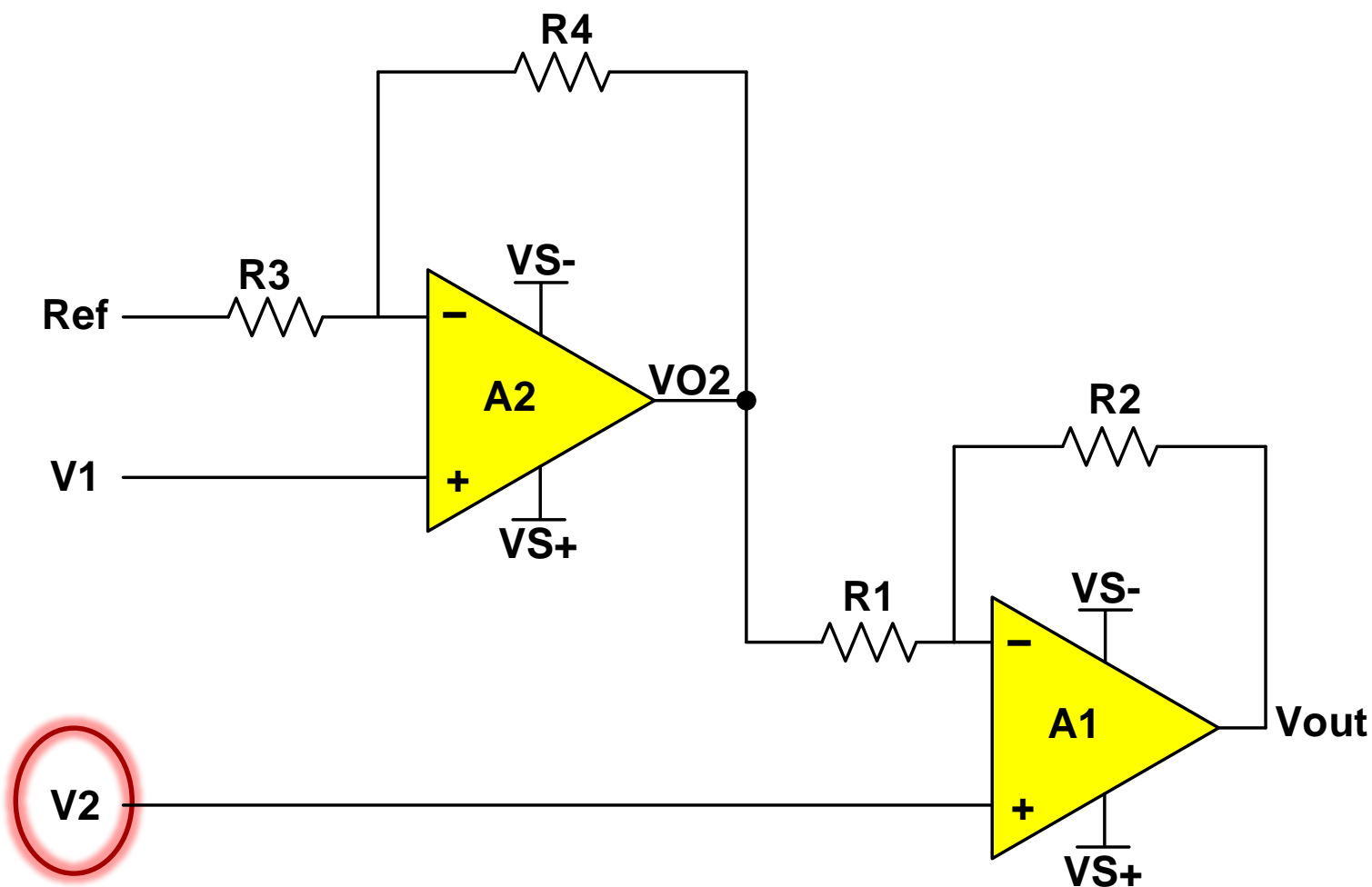
**Ground VO2:**

Looks like non-inverting configuration,

$$V_{out} = \left( 1 + \frac{R2}{R1} \right) \times V2$$

Equation V2\*

# IA topologies – 2 amp IA derivation; A1 derivation



Derive output of A1 using superposition theorem:

Equation	V2	VO2
V2*	Keep	Short
VO2*	Short	Keep
<b><math>V_{out} = V2^* + VO2^*</math></b>		

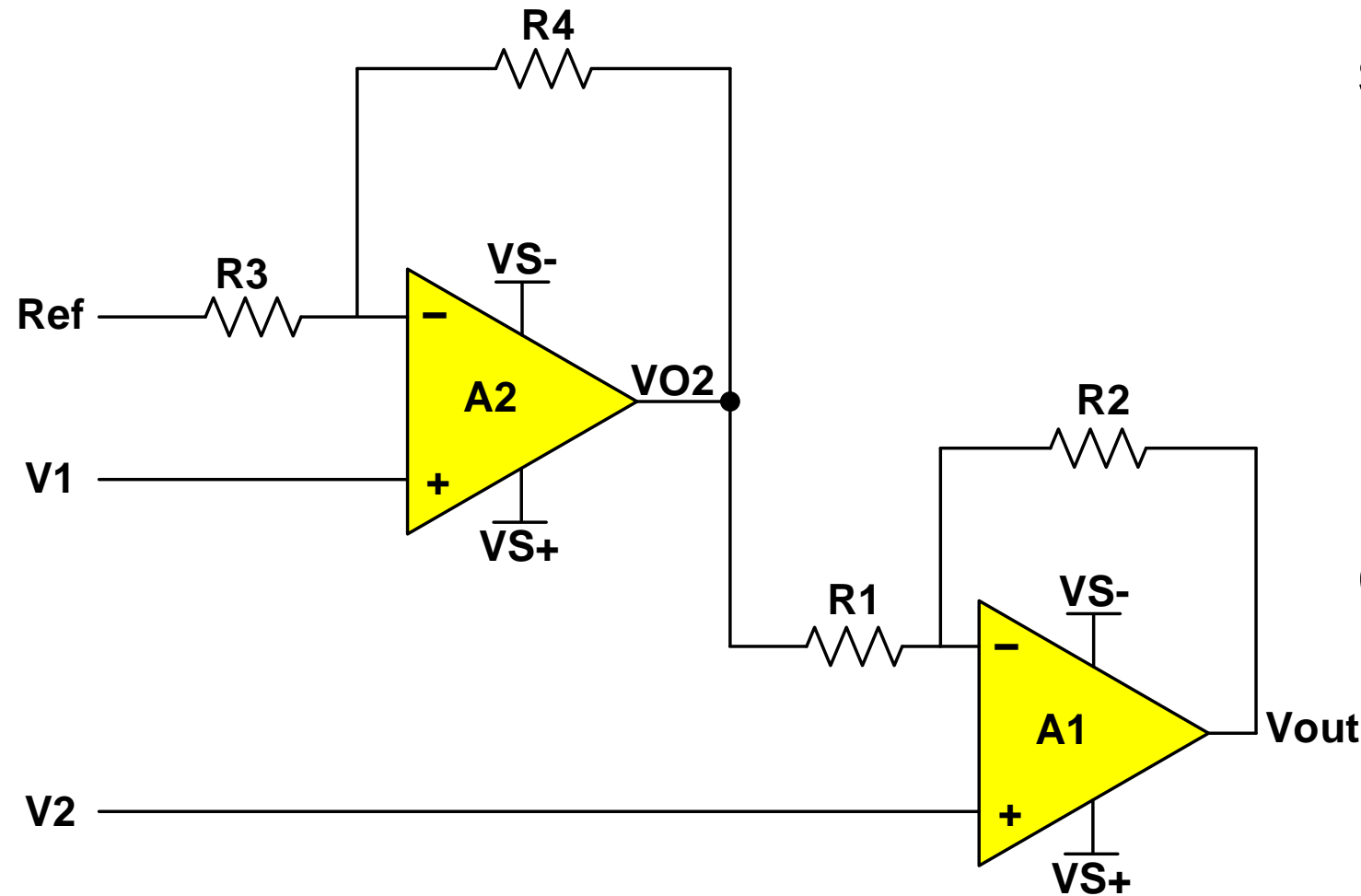
**Ground V2:**

Looks like an inverting configuration,

$$V_{out} = \frac{-R2}{R1} \times VO2$$

Equation VO2\*

# IA topologies – 2 amp IA derivation; A1 derivation



Derive output of A1 using superposition:

Equation	V2	VO2	
V2*	Keep	Short	$V2^* = \left(1 + \frac{R2}{R1}\right) \times V2$
VO2*	Short	Keep	$VO2^* = \frac{-R2}{R1} \times VO2$
<b><math>Vout = V2^* + VO2^*</math></b>			

Combine V2\* and VO2\* to yield Vout:

$$Vout = \left(1 + \frac{R2}{R1}\right) \times V1 - \frac{R2}{R1} \times VO2 \text{ (eq1)}$$

$$VO2 = \frac{-R4}{R3} \times Ref + \left(1 + \frac{R4}{R3}\right) \times V1 \text{ (eq2)}$$

$$Vout = \left(1 + \frac{R2}{R1}\right) \times V2 - \frac{R2}{R1} \times \left[ \frac{-R4}{R3} \times Ref + \left(1 + \frac{R4}{R3}\right) \times V1 \right]$$

# IA topologies – 2 amp IA derivation; simplified

$$V_{out} = \left(1 + \frac{R2}{R1}\right) \times V2 - \frac{R2}{R1} \times \left[ \frac{-R4}{R3} \times Ref + \left(1 + \frac{R4}{R3}\right) \times V1 \right]$$

Assuming  $R4 = R1$  and  $R3 = R2$ :

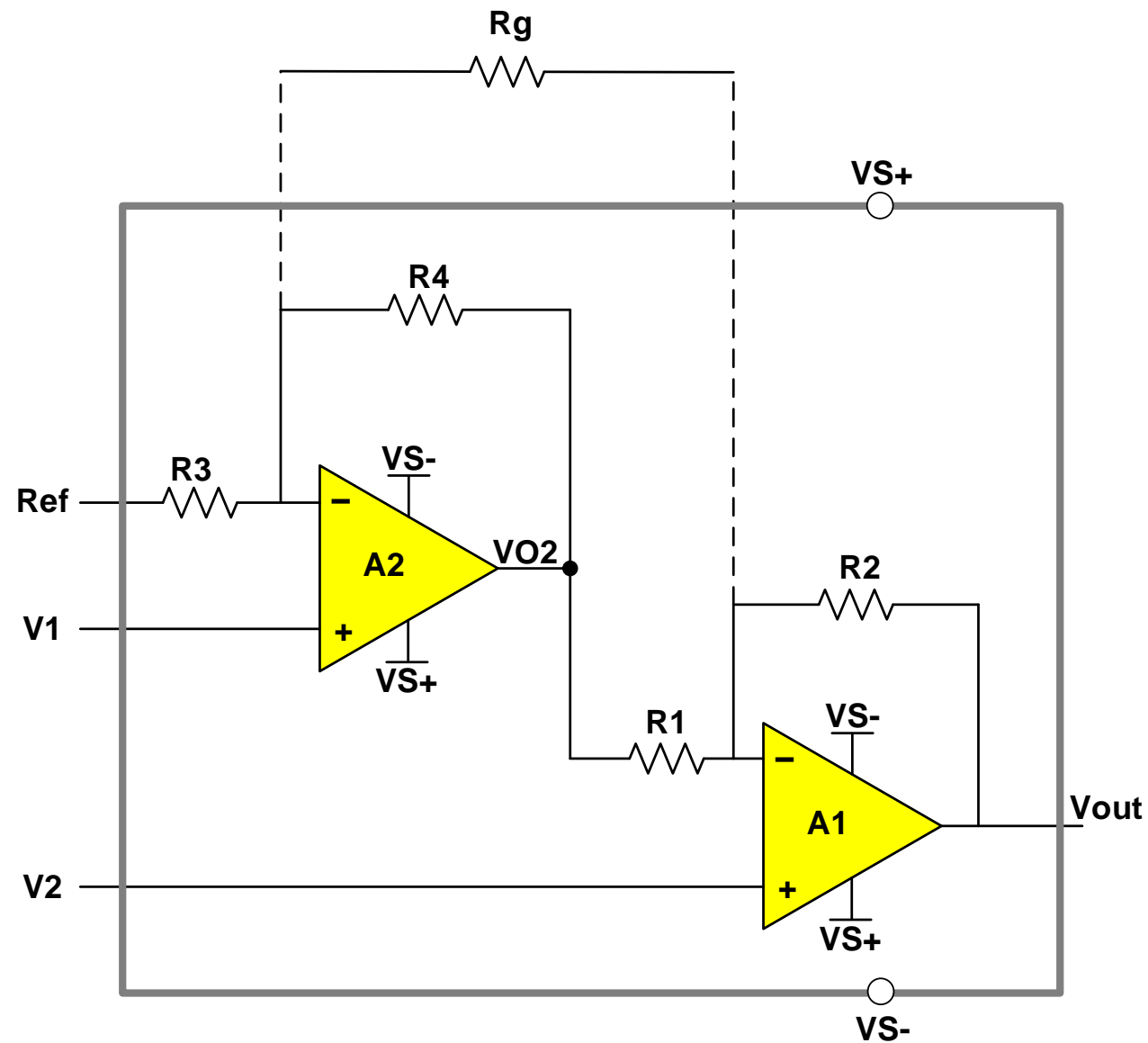
$$V_{out} = \left(1 + \frac{R2}{R1}\right) \times V2 - \frac{R2}{R1} \times \left[ \frac{-R1}{R2} \times Ref + \left(1 + \frac{R1}{R2}\right) \times V1 \right]$$

Simplify...

$$V_{out} = \left(1 + \frac{R2}{R1}\right) \times (V2 - V1) + Ref$$

Ad                      Vd

# 2 amp IA – Gain control & driving the Ref pin



**Goal:** Set the gain of the entire circuit with one additional resistor

Adding resistor Rg yields the following output equation:

$$V_{out} = \left( 1 + \frac{R2}{R1} + \frac{2 \times R2}{Rg} \right) \times (V2 - V1) + Ref$$

**Resistor matching recap:**

Aim for  $R4 = R1$  and  $R3 = R2$

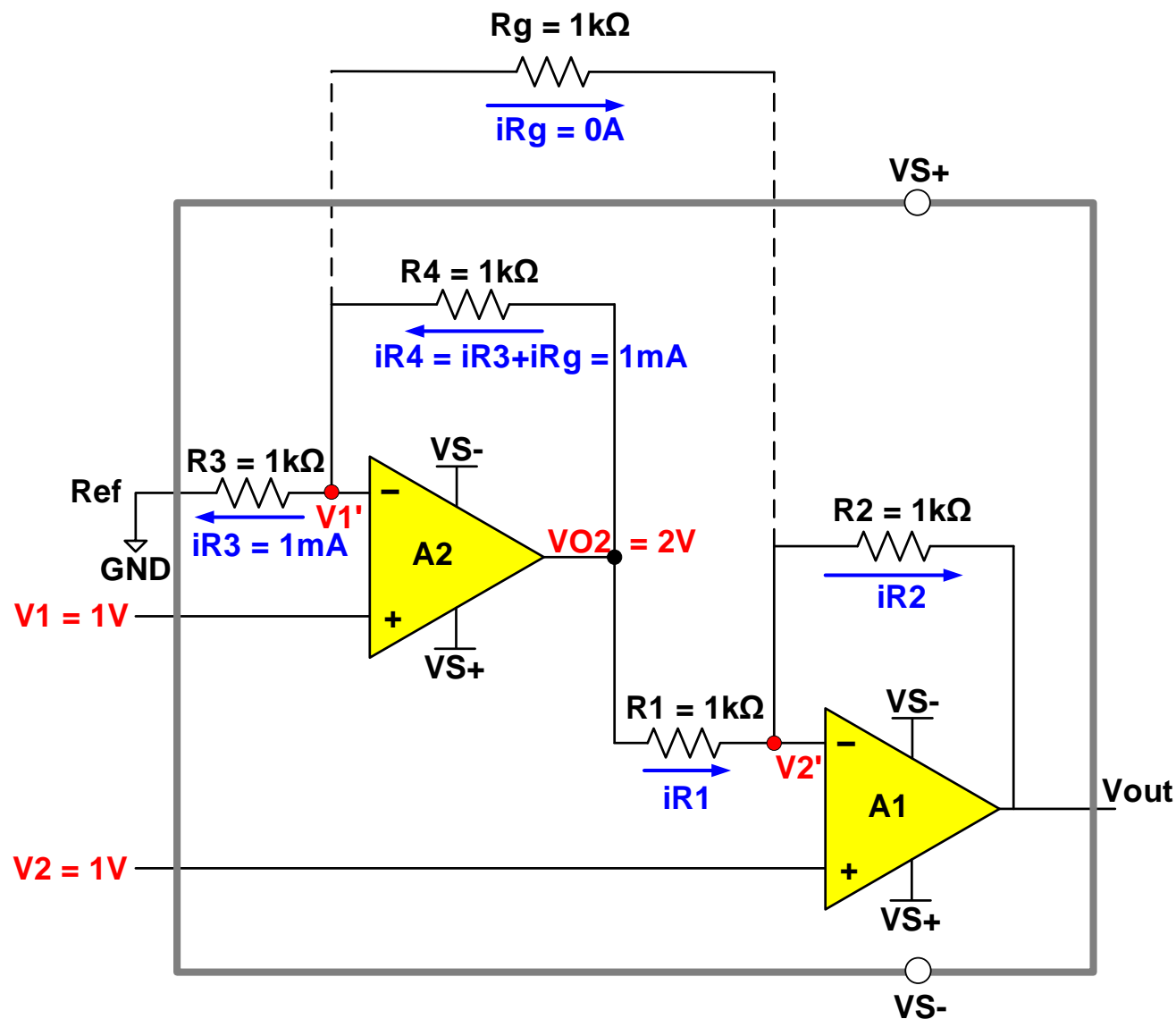
In an integrated solution, R1, R2, R3, and R4 are absolutely matched in production.

**Reference voltage recap:**

Drive with low-impedance source, such as a buffer or voltage reference

# 2 amp IA – ACM analysis and performance

$$\text{Common mode gain} = A_{CM} = \frac{V_{OCM}}{V_{CM}} \ll 1$$



Apply a 1V VCM (1V at V1 and V2)

Assume:

- Ref is grounded
- R1, R2, R3, R4 and Rg = 1kΩ

If  $V1 = 1V \rightarrow V1' = 1V$ :

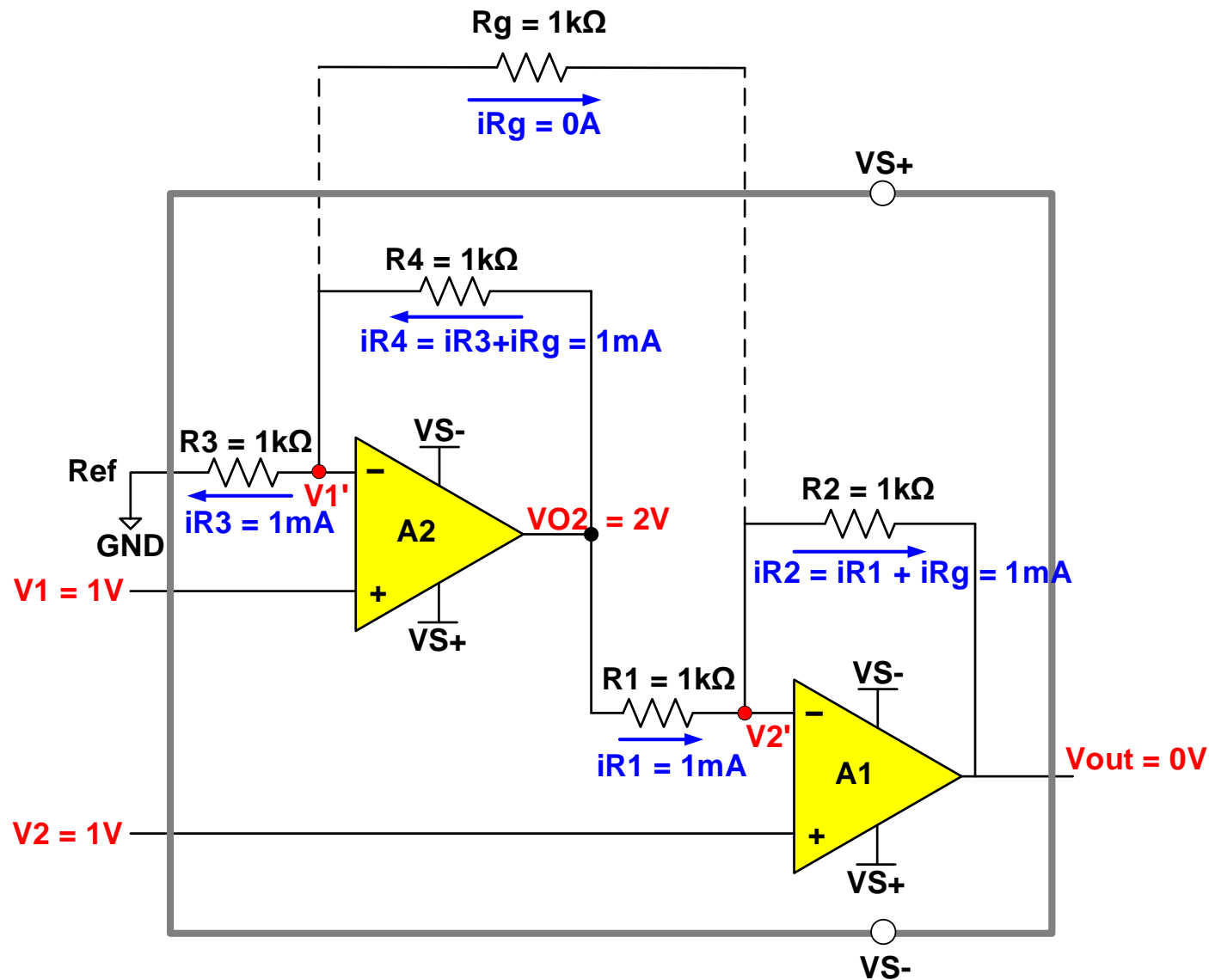
- Current flowing through R3 =  $1V/1k\Omega = 1mA$

If  $V2 = 1V \rightarrow V2' = 1V$ :

- $V1' = V2' = 1V$ , there is no current flowing through Rg, so  $iRg = 0A$

- $iR4 = iR3 + iRg = 1mA$ ,
  - Voltage drop across R4 is 1V, so  $VO2 = 2V$

# 2 amp IA – ACM analysis and performance cont'd



$V_{O2} = 2V$  and  $V_2' = 1V$ :

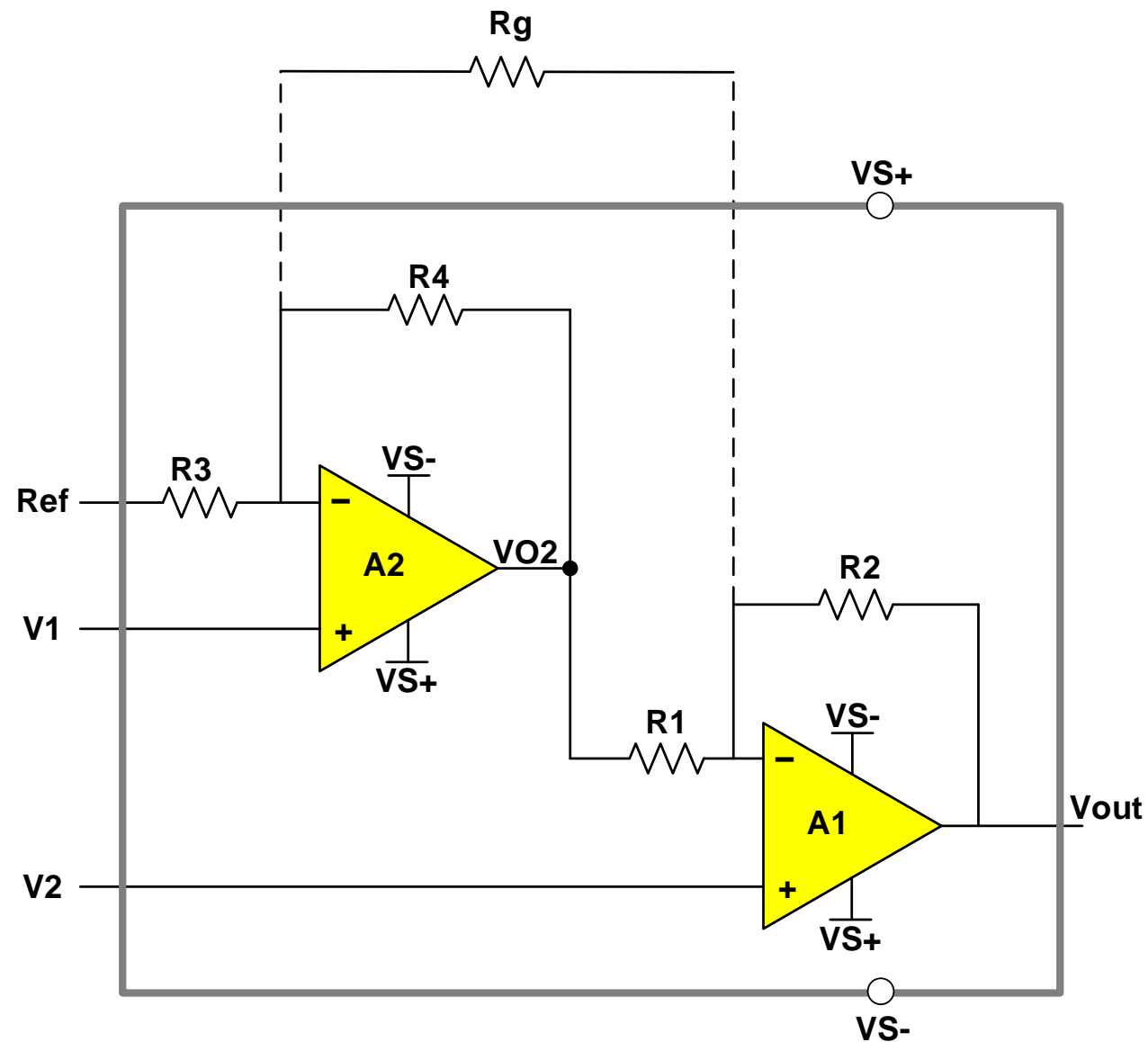
– current flowing through  $R_1$  is  $1V/1k\Omega = 1mA$

$iR_2 = iR_g + 1mA = 1mA$

Voltage drop across  $R_2$  is  $1V$ , so  $V_{out} = 0V$

**The two-amp IA was able to reject the common mode voltage (VCM)**

# 2 amp IA topology drawbacks – Gain



$$V_{out} = \left( 1 + \frac{R2}{R1} + \frac{2 \times R2}{Rg} \right) \times (V2 - V1) + Ref$$

$$A_d = \text{differential gain} = 1 + \frac{R2}{R1} + \frac{2 \times R2}{Rg}$$

$$V_d = \text{differential voltage} = V2 - V1$$

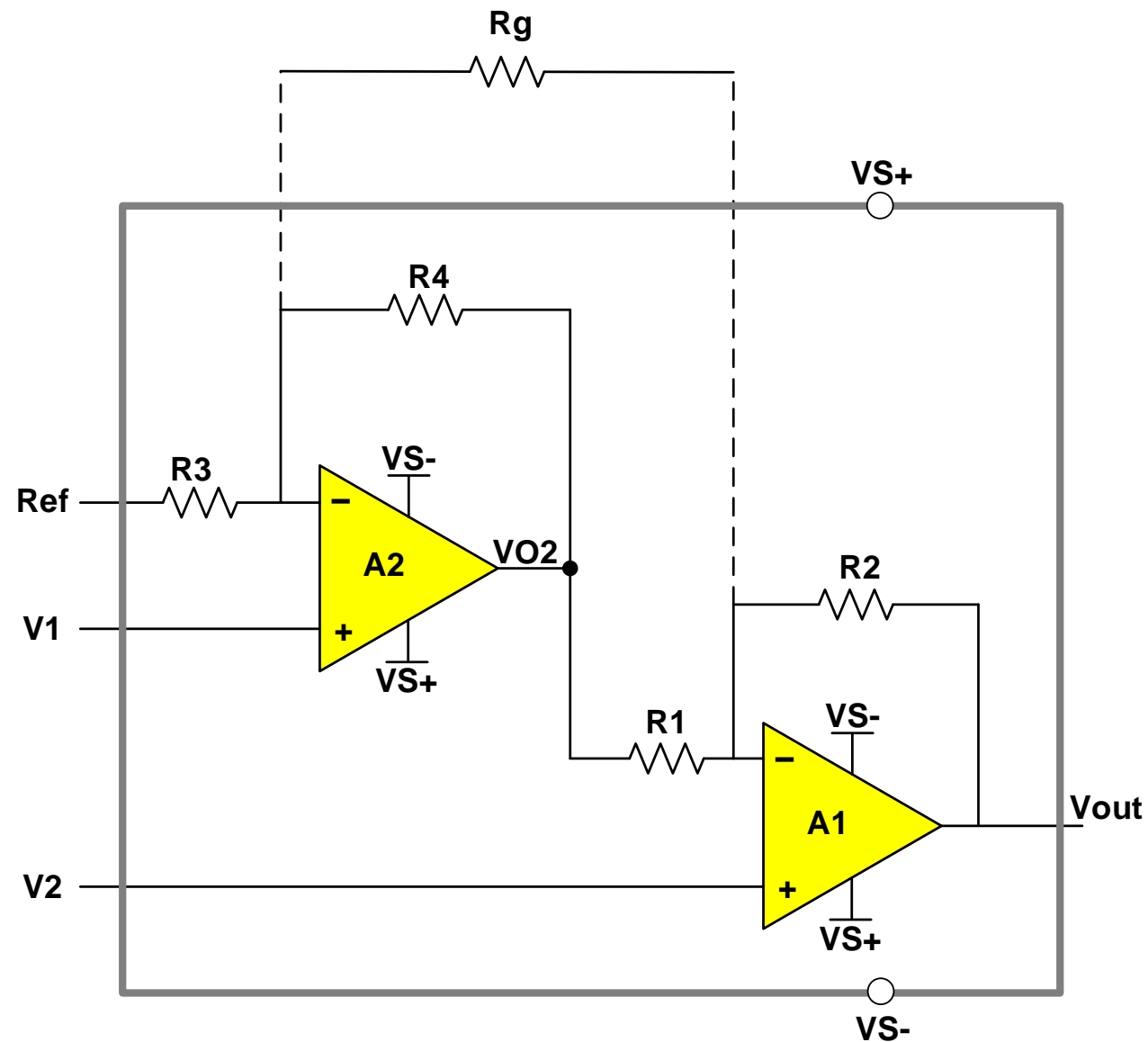
Ref = reference voltage, level shifting term

## Drawback:

- $A_d$  cannot be 1V/V due to the addition of 1 in the gain equation:  $1 + \frac{R2}{R1} + \frac{2 \times R2}{Rg}$



# 2 amp IA topology drawbacks – Headroom



$$V_{out} = \left( 1 + \frac{R2}{R1} + \frac{2 \times R2}{Rg} \right) \times (V1 - V2) + Ref$$

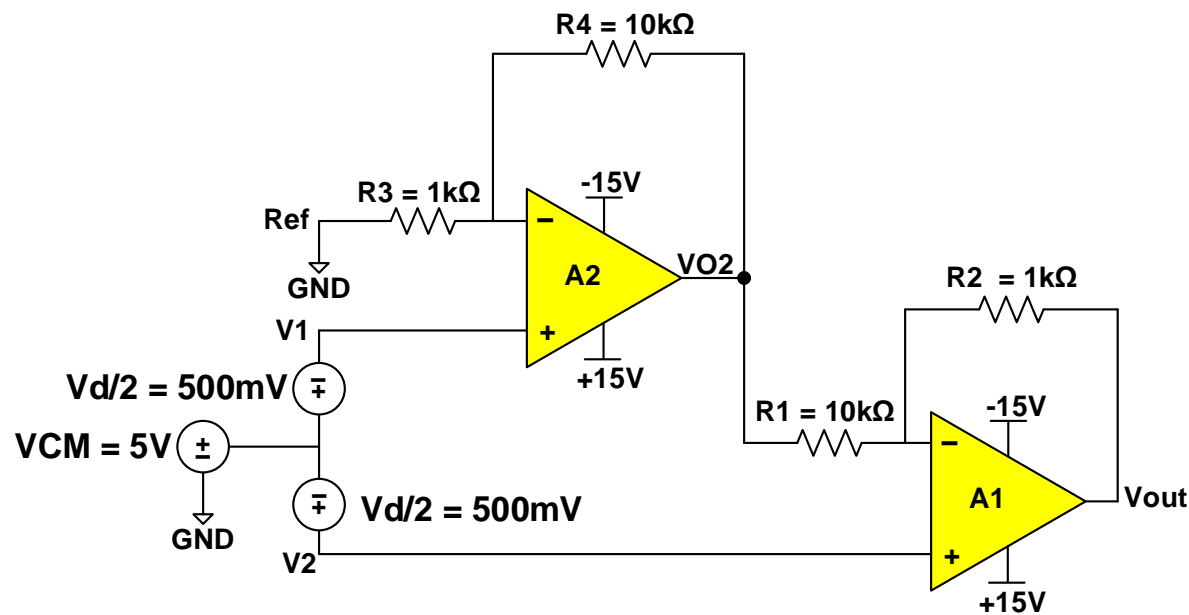
## Drawback:

- Headroom:
  - Low gain: If  $R4 \gg R3$ , A2 will saturate if  $V1$  VCM is too high, leaving no headroom for A2 to amplify the wanted signal
  - High gain: If  $R4 \ll R3$ , there is more headroom at VO2, allowing for higher VCM

\*Note: Ref = 0V

# 2 amp IA topology drawbacks – Headroom cont'd

$$V_{out} = \left( 1 + \frac{R_2}{R_1} + \frac{2 \times R_2}{R_g} \right) \times (V_d) + Ref$$



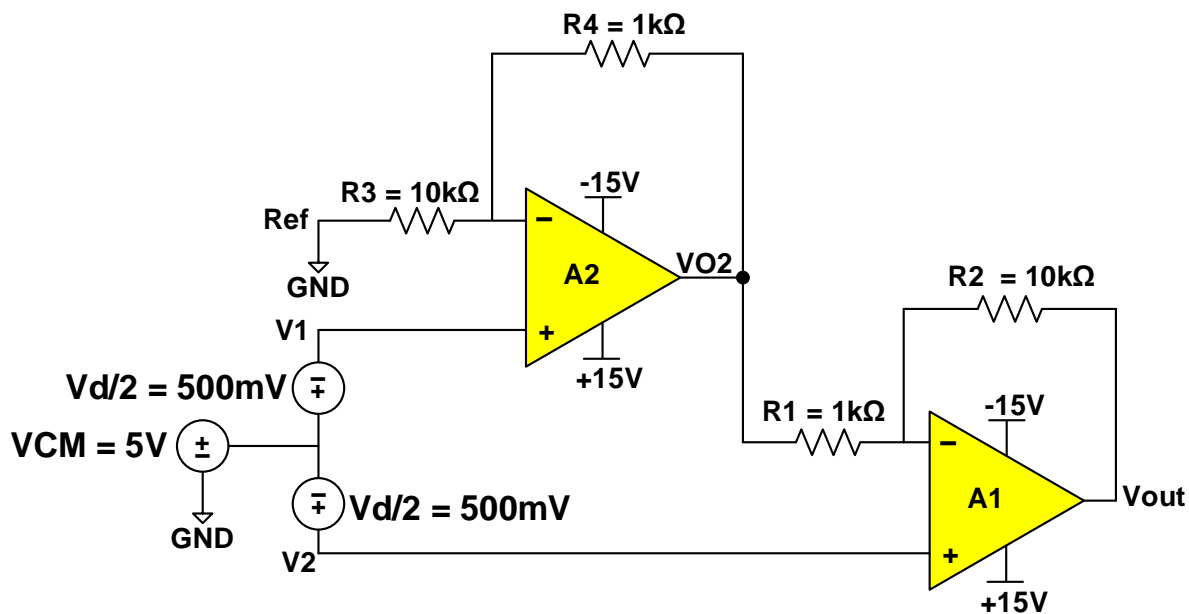
**Low gain example:  $R_4 \gg R_3$**

Assume A1 and A2 are powered by  $\pm 15V$  supplies

$A_d = 1.1 \text{ V/V}$ ,  $V_d = 1V$

$V_{CM} = 5 \text{ V}$ ,  $Ref = 0V$

Expected output  $V_{out} = A_d \times V_d + Ref = 1.1 \text{ V}$



**High gain example:  $R_4 \ll R_3$**

Assume A1 and A2 are powered by  $\pm 15V$  supplies

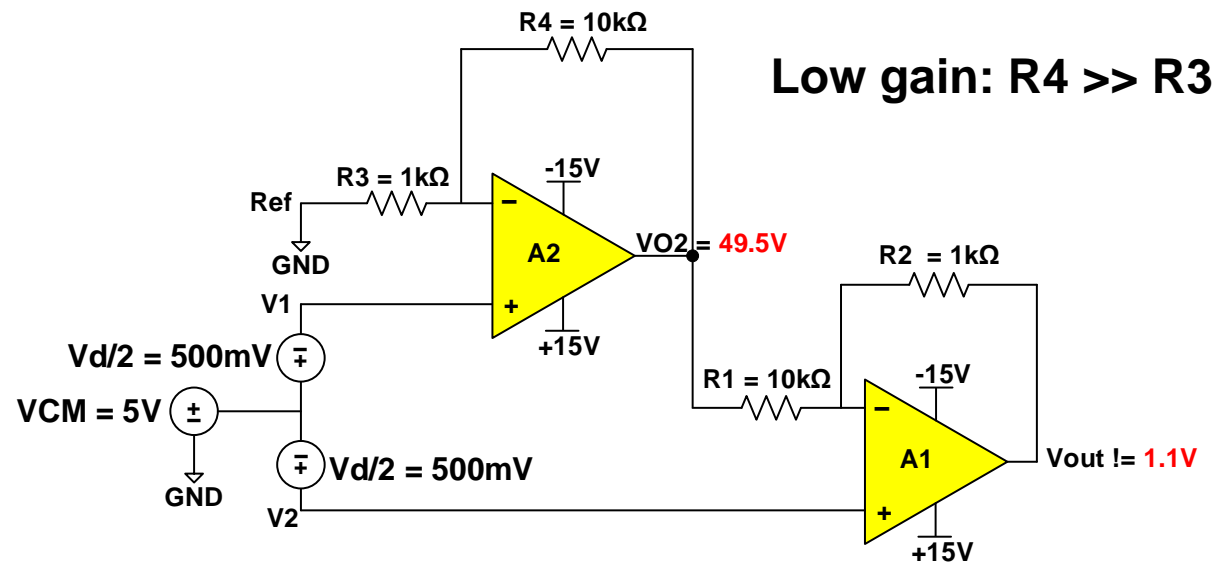
$A_d = 11 \text{ V/V}$ ,  $V_d = 1V$

$V_{CM} = 5 \text{ V}$ ,  $Ref = 0V$

Expected output  $V_{out} = A_d \times V_d + Ref = 11 \text{ V}$

# 2 amp IA topology drawbacks – Headroom cont'd

$$V_{out} = \left( 1 + \frac{R_2}{R_1} + \frac{2 \times R_2}{R_g} \right) \times (V_d) + Ref$$



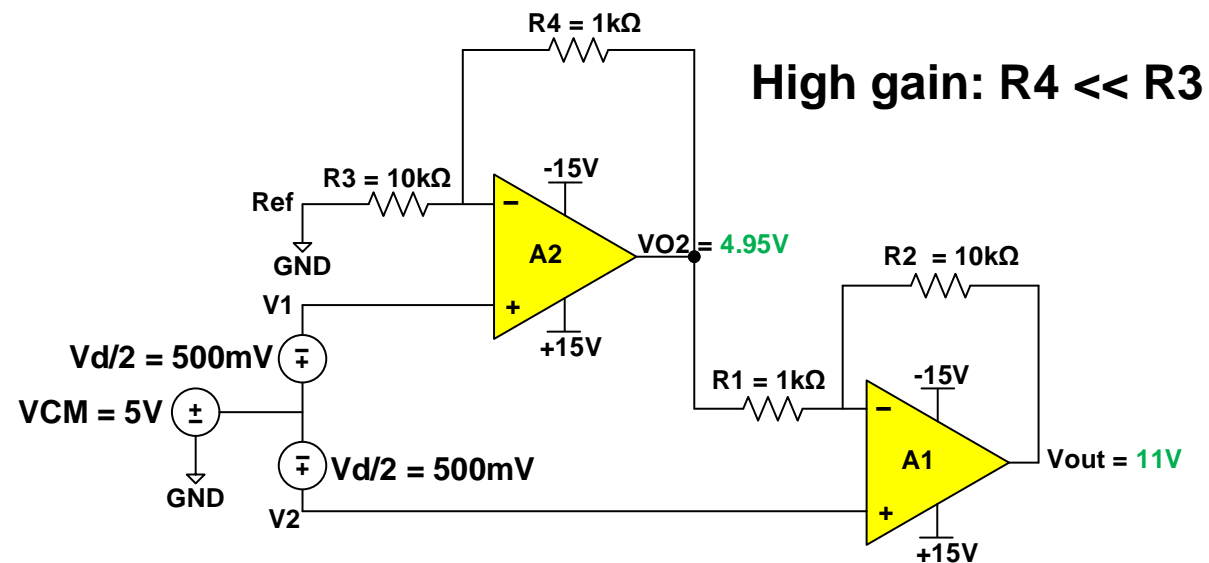
A1 and A2:  $\pm 15V$  supplies, RRIO

Ad = 1.1 V/V, Vd = 1V, VCM = 5V, Ref = 0V

Expected output Vout = Ad  $\times$  Vd + Ref = 1.1 V

VO2 = 49.5V

Vout != 1.1V



A1 and A2:  $\pm 15V$  supplies, RRIO

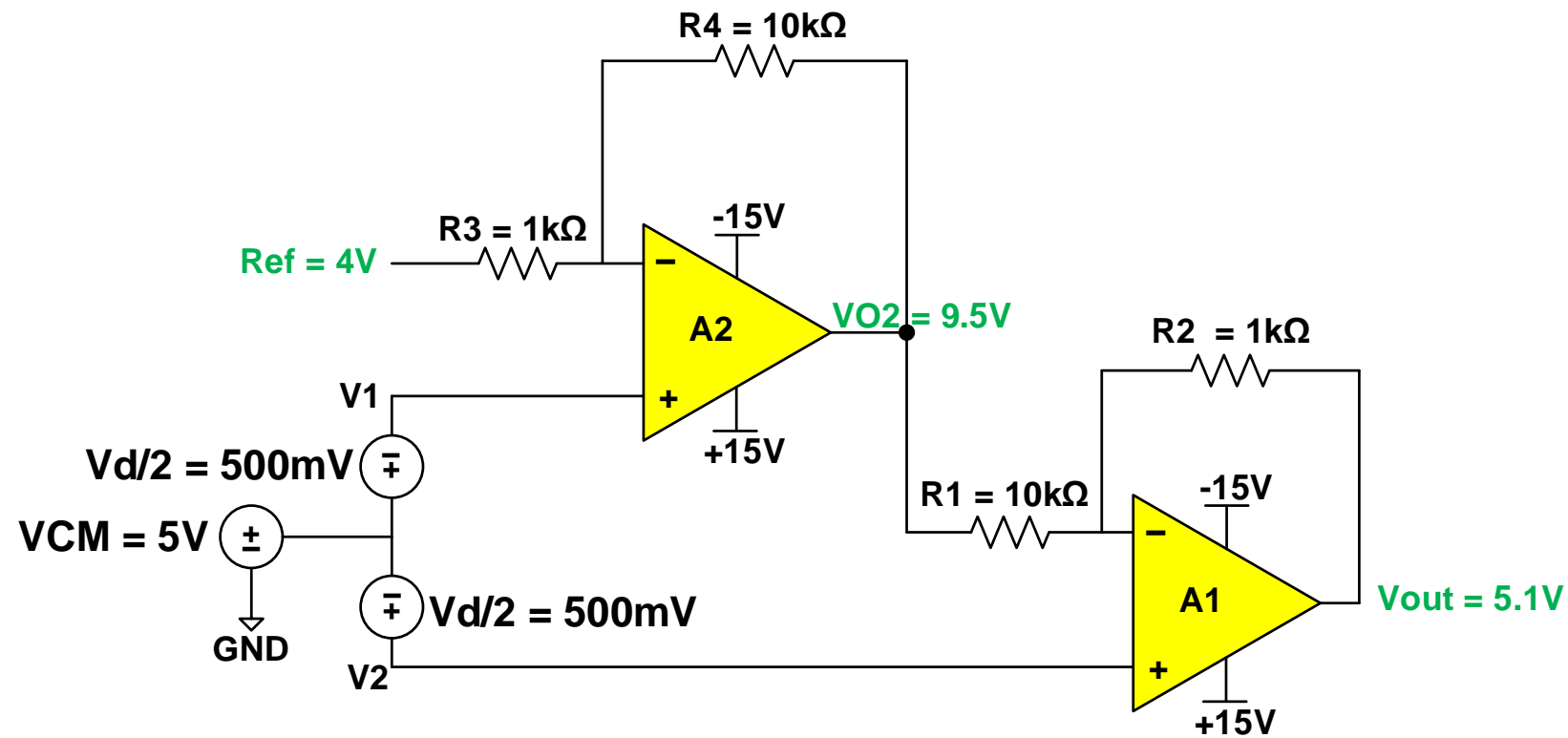
Ad = 11 V/V, Vd = 1V, VCM = 5V, Ref = 0V

Expected output Vout = Ad  $\times$  Vd + Ref = 11 V

VO2 = 4.95V

VOUT = 11V

# 2 amp IA topology drawbacks – Headroom cont'd



## Low gain: $R4 \gg R3$

- A1 and A2:  $\pm 15V$  supplies, RRIO
- Differential gain ( $A_d$ ) = 1.1 V/V
- Differential voltage ( $V_d$ ) = 1V
- Common mode voltage ( $V_{CM}$ ) = 5V
- Reference voltage ( $Ref$ ) = 4V

## Expected output:

$$V_{out} = A_d \times V_d + Ref = 5.1 \text{ V}$$

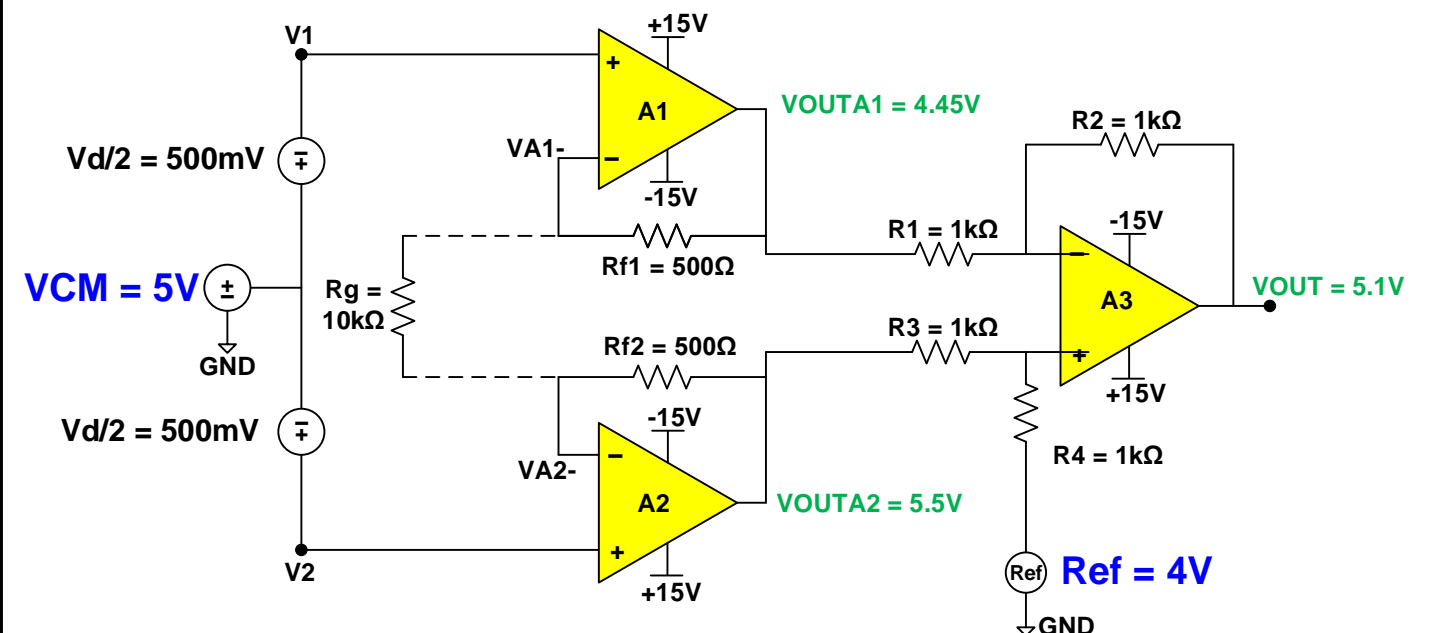
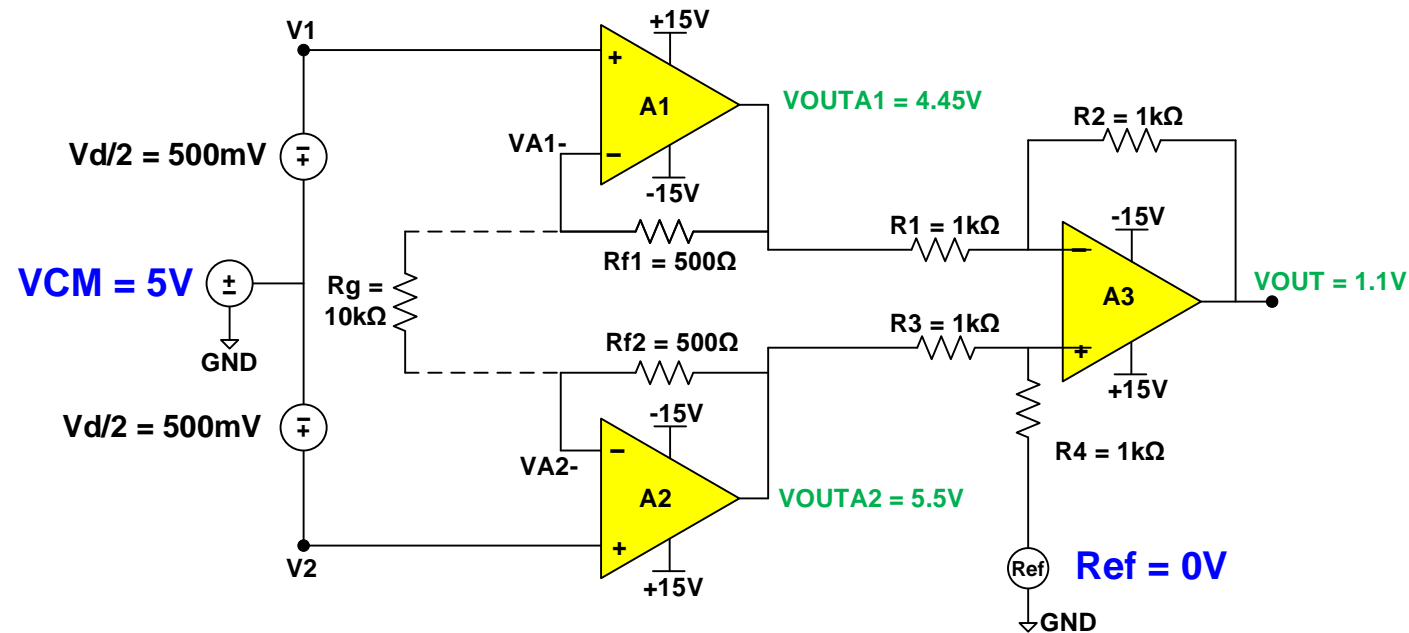
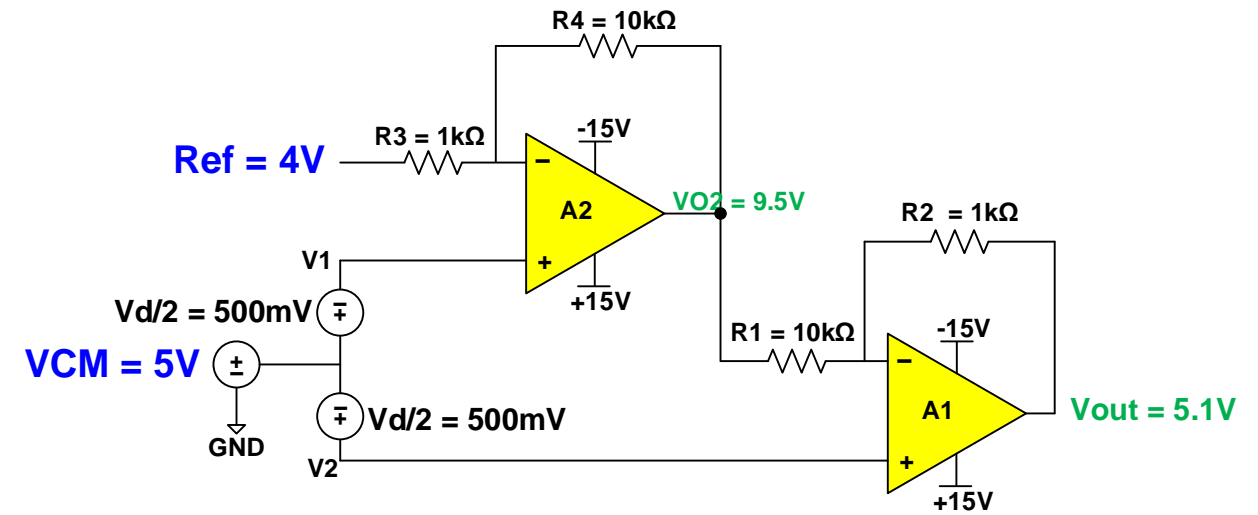
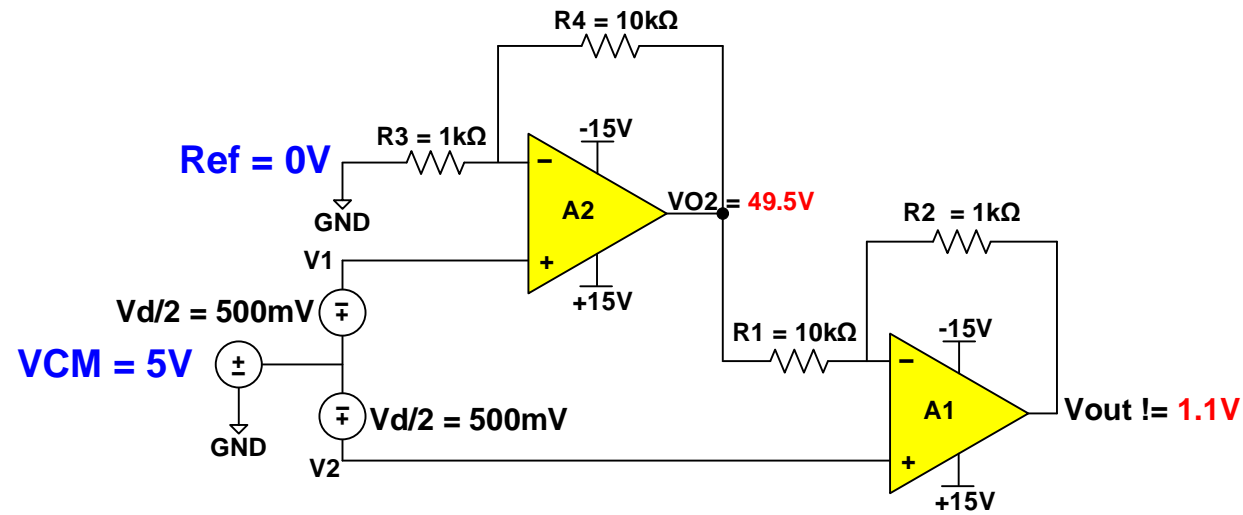
$$VO_2 = 9.5V$$

$$V_{out} = 5.1V$$

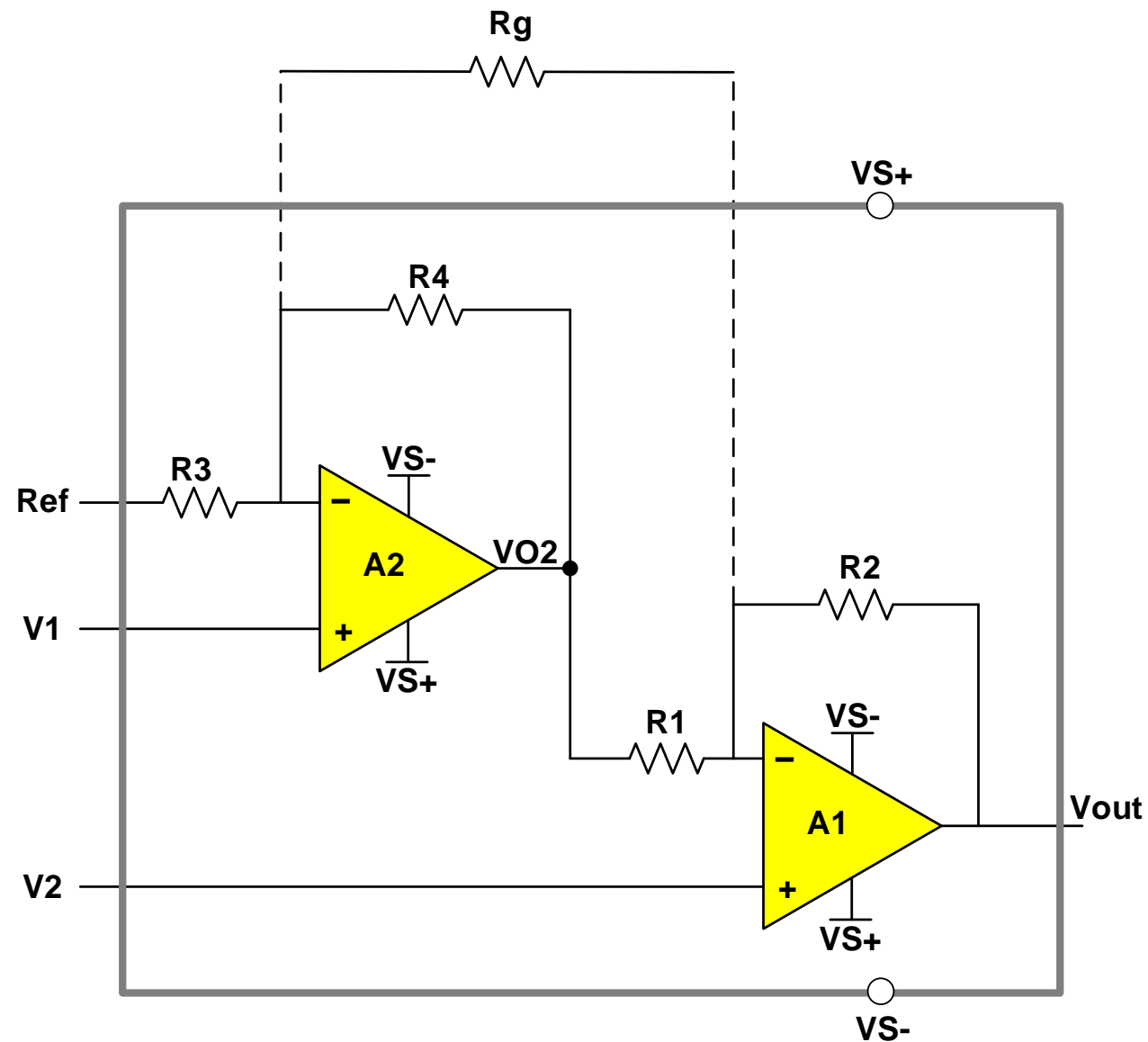
$$V_{out} = \left( 1 + \frac{R_2}{R_1} + \frac{2 \times R_2}{R_g} \right) \times (V_d) + Ref$$

# 2 amp IA vs 3 amp IA – Headroom

$A_d = 1.1V/V$ ,  $V_d = 1V$ ,  $V_{CM} = 5V$   
 $Ref = 0V$  or  $4V$   
 Expected  $V_{out} = 1.1V$  or  $5.1V$



# 2 amp IA topology drawbacks – AC CMRR



## Drawback:

- AC CMRR:
  - Path from  $V_1$  to  $V_{out}$  has an additional phase shift of A2

## Example:

Assume we apply  $V_{CM}$  at  $F_{CM}$  to  $V_1$  and  $V_2$ . Expected common mode error = 0V which means A1 needs to see 0 difference between  $V_2$  and  $VO_2$ .

Phase shift introduced by A2 causes the phase of  $VO_2$  to lag behind  $V_2$  → frequency-dependent common mode voltage error at  $V_{out}$

# 2 amp IA – Example

Assume the following conditions:

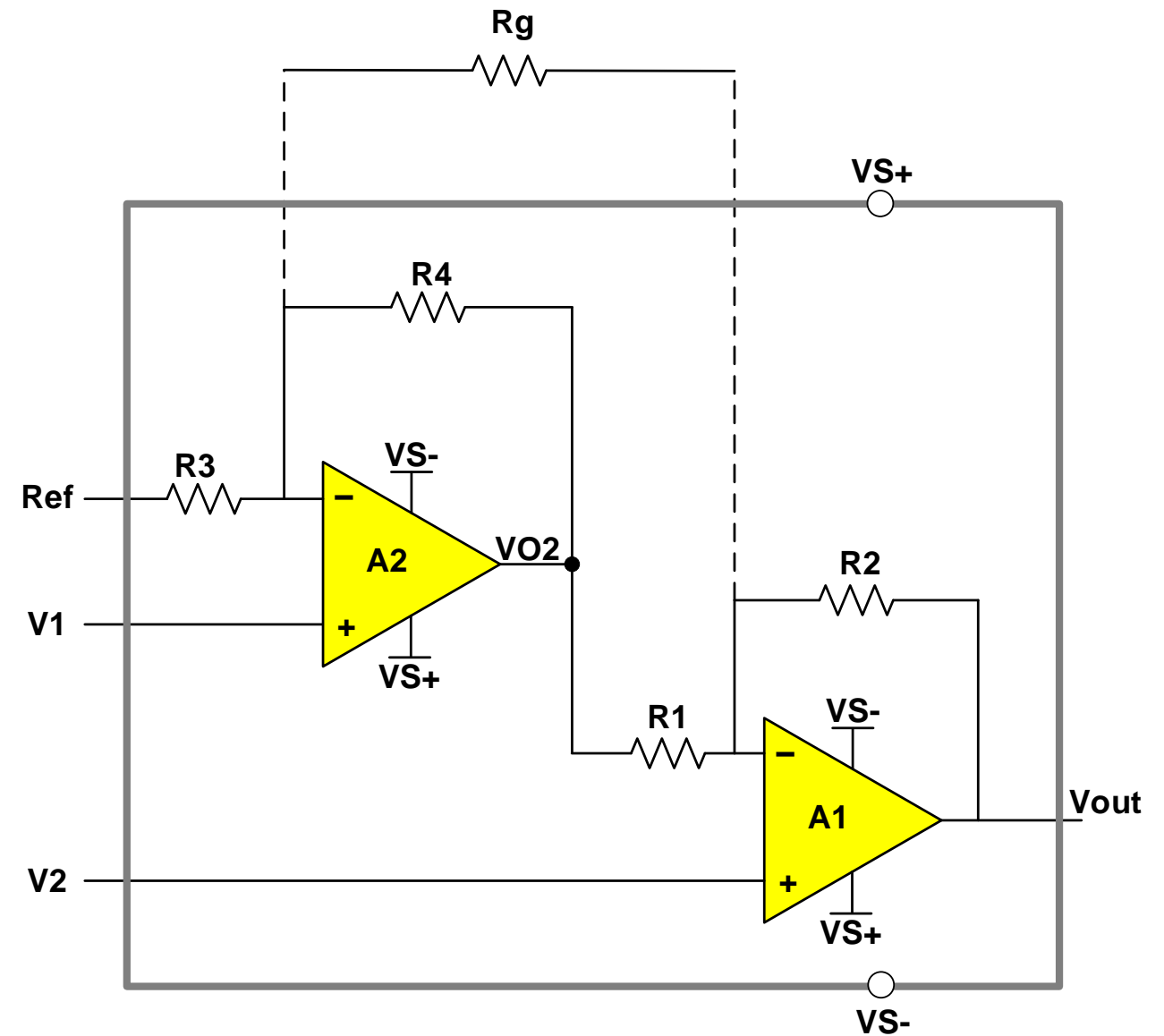
Voltage supplies =  $\pm 10V$ , Ref = 0V

$V_d = 10mV$ ,  $V_{CM} = 2V$

Expected  $V_{out} = 3V$

## 4 design steps:

1. Determine gain required
2. Find IA & check boundary plot
3. Determine  $R_g$  required
4. Build and simulate with confidence



# 2 Amp IA – Example cont'd

## 1. Determine gain required

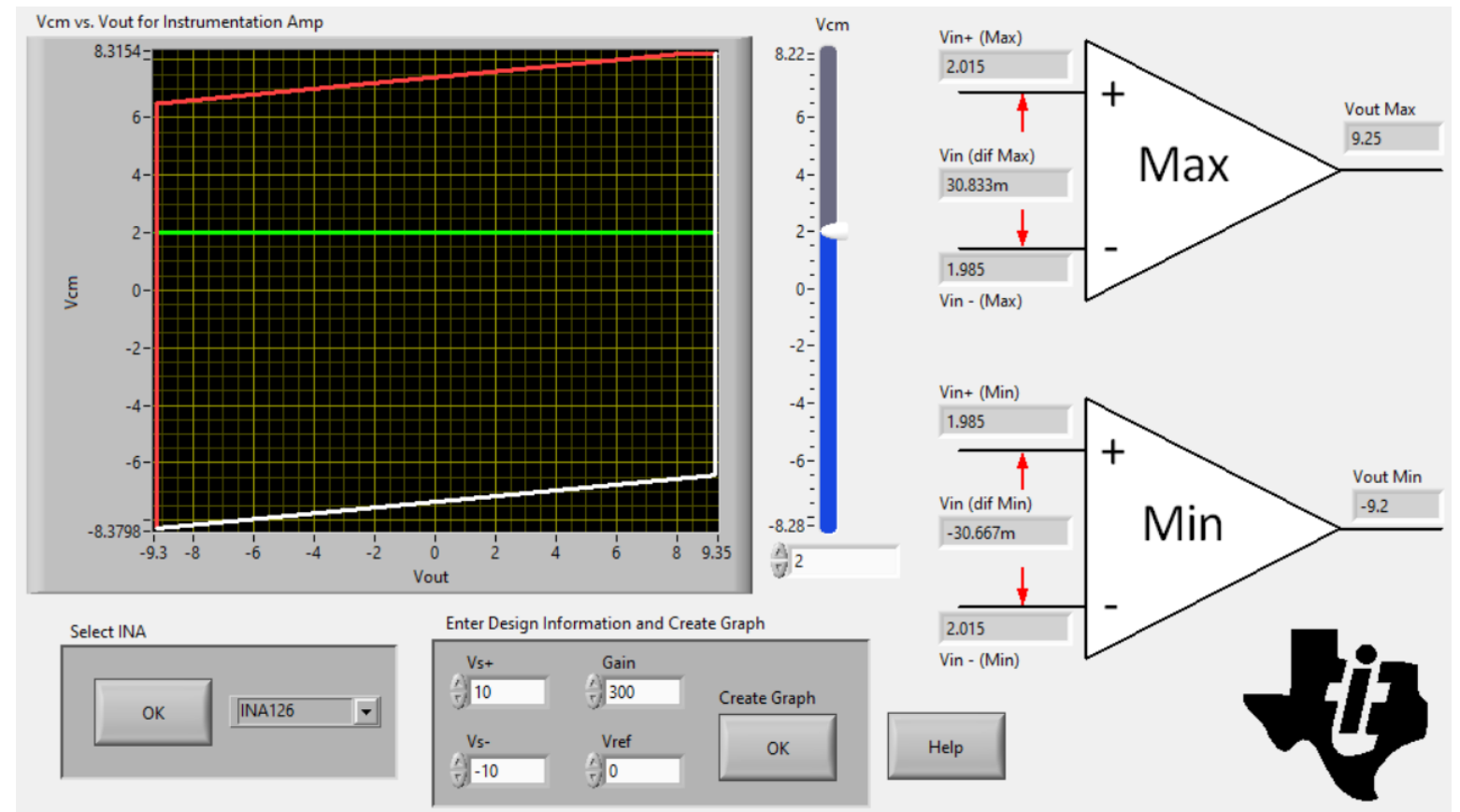
$$\text{Gain} = \frac{\Delta V_{out}}{\Delta V_{in}} = \frac{3V}{10mV} = 300V/V$$

## 2. Find IA & check boundary plot

IA selected: INA126

Plug in supply, gain, ref and VCM

Make sure our expected input & output voltages are within range



[Analog engineer's calculator → INA VCM vs Vout](#)

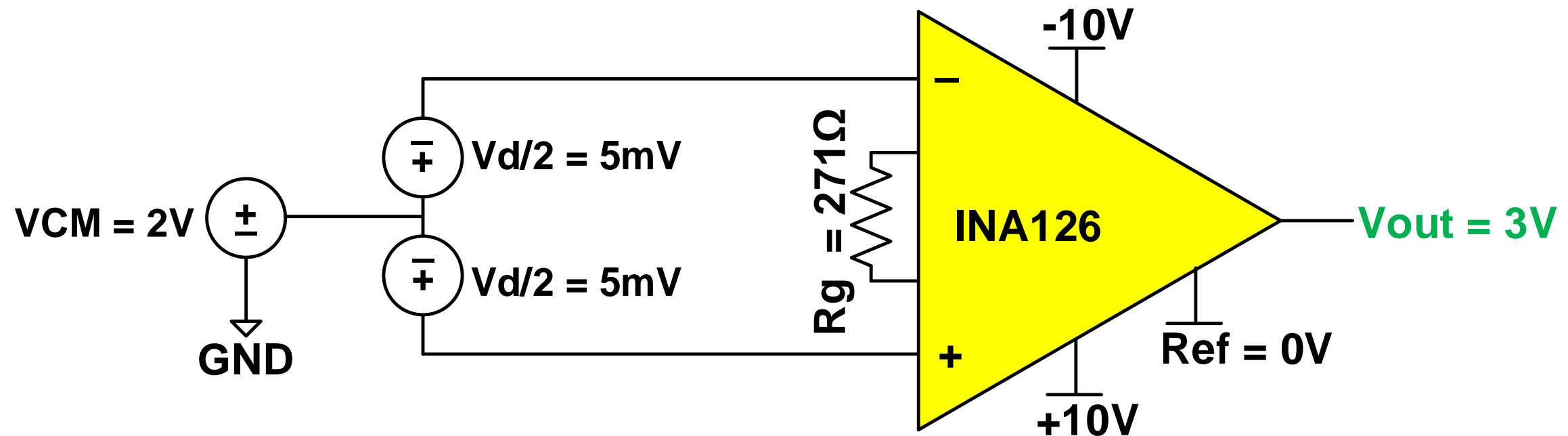


## 2 amp IA – Example cont'd

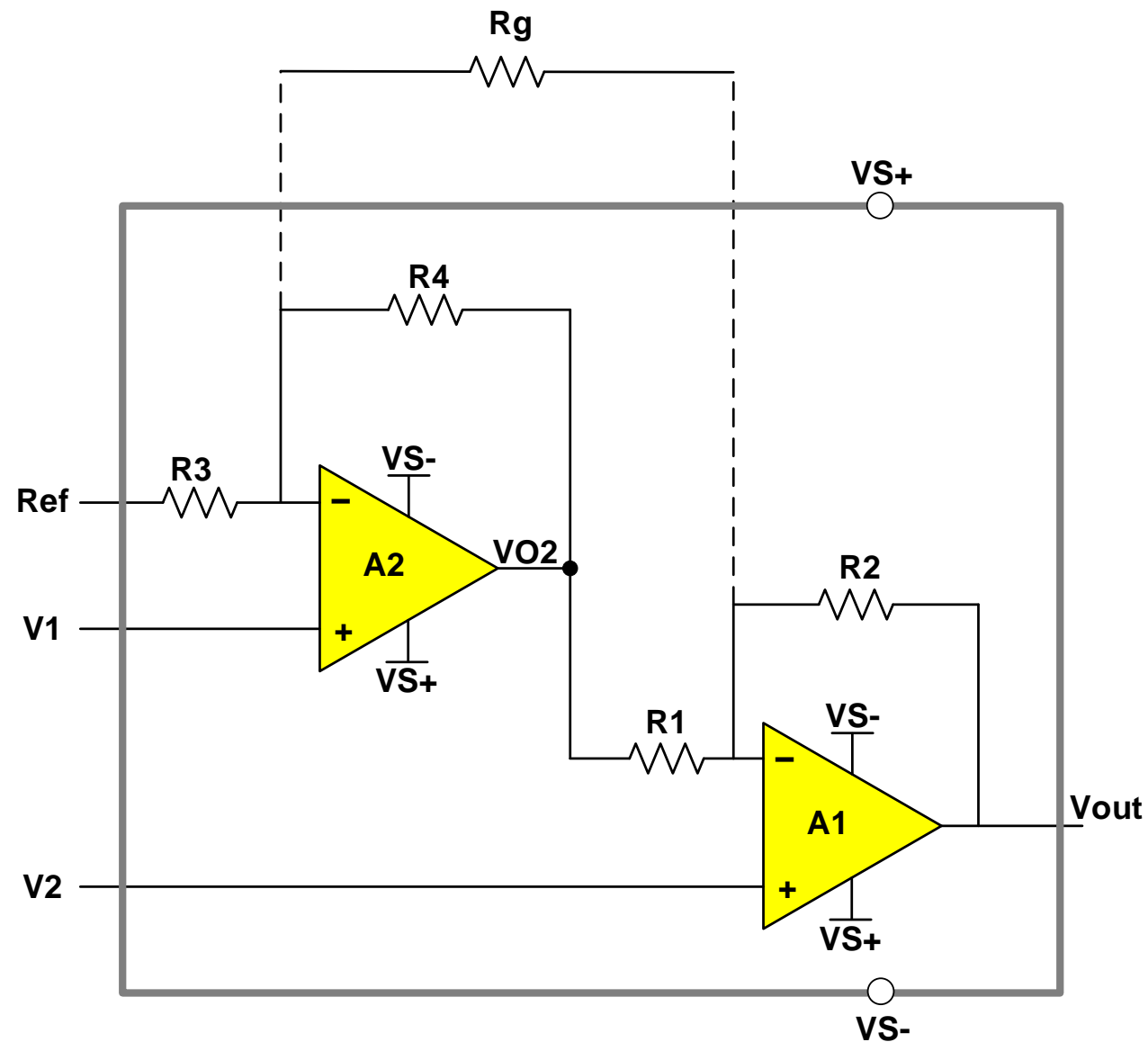
### 3. Determine $R_g$ required

$$\text{INA126 datasheet} \rightarrow \text{Gain} = 5 + \frac{80k}{R_g} \rightarrow R_g = 271\Omega$$

### 4. Build and simulate with confidence



# 2 amp IA – Summary of benefits and drawbacks



## Benefits:

- Fewer resistors, must need to be well matched → pick an integrated IA
- Fewer amplifiers → lower cost
- High input impedance

## Drawbacks:

- Minimum gain limitation ( $> 1V/V$  minimum)
- Gain vs headroom
- CMRR vs frequency
- Common mode voltage must be within the power supply rails

**Thanks for your time!**  
**Please try the quiz.**

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